

# Evaluation of seismic capacity and response according to the nonlinear modeling approach of members in steel moment frames

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## Abstract

In this paper, the aim is to evaluate the seismic behavior of steel moment frames by nonlinear static analysis and incremental dynamic analysis. In this regard, 5 and 10 story frames in both intermediate and special ductility have been used. Since the type of sections and elements used in modeling are among the parameters that affect the behavior of the structure, in this study, which was performed using OpenSees software, fiber sections were used for two types of beam elements. Non-linear column (distributed plasticity) and articulated beam element (concentrated plasticity) are used. The results of the analysis show that the ratio of the collapse capacity of the frames to each other varies between 1% to 6%. On the other hand, by deepening the research on one of the frames, it was shown that the stiffness ratio between the end springs and the middle member will affect the difference between the collapse capacity shown in the analysis.

**Keywords:** moment Frame, Concentrated Plasticity Approach, distributed Plastic Approach, Incremental Dynamic Analysis, Collapse

## Introduction

A catastrophe is an event that is usually "sudden" that causes undesirable changes and changes in objects and creatures that result in disruption of the natural pattern of life. Earthquake is one of these catastrophes and natural disasters. Buildings that according to regulations to Earthquake resistance is designed, it must remain in the linear range due to dead and live gravity due to the use of the building, but due to the occurrence of catastrophic events such as earthquakes can be from the capacity of the structure in the nonlinear range even up to the collapse threshold due to maximum Use possible ground movements, especially for structures with residential use.

If structural members are likely to enter the nonlinear range, a distributed or concentrated approach can generally be chosen for each member. In the extended approach, as the load increases, the internal stresses of each element along the member reach the yield stress, nonlinear expansion along the member occurs through redistribution.

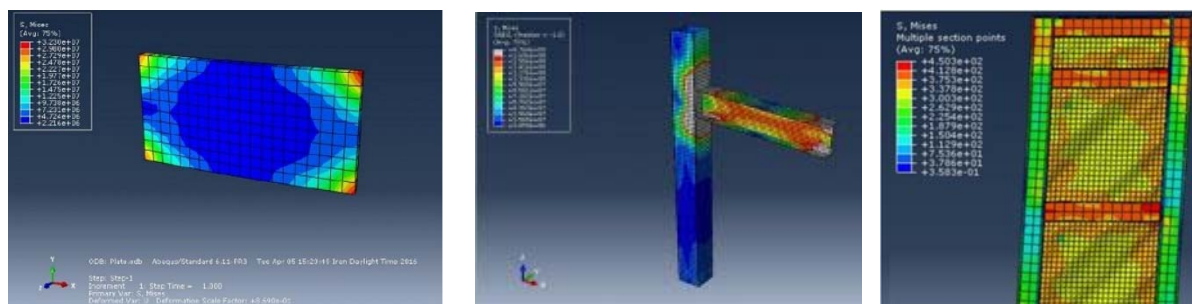


Fig 1:Expansion of plasticity joint length in different structural members

In the concentrated approach, however, by considering a fixed location for zero-length plastic joints, forces and displacements are evaluated according to the tolerable strength of the material, and in other places a linear behavior is assumed for that structural member.

Nonlinear behavior can be modeled with both strain stress equations and displacement forces, or a combination of both approaches. The types of analysis that can be considered are classified according to the appearance of nonlinear behavior in materials (elastic or inelastic) or in the geometry of the members, the most accurate of which is according to Figure 2 non-linear inelastic behavior. [1]

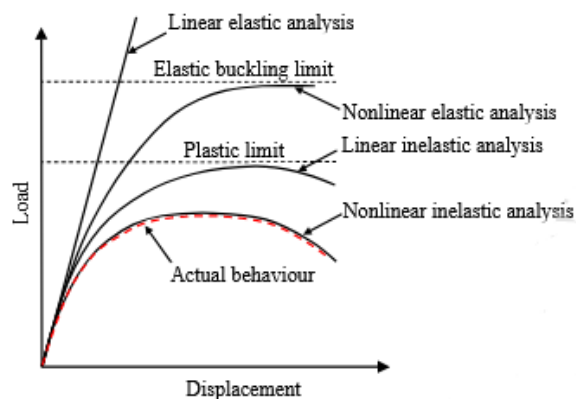


Fig 2: Comparison of nonlinear behavioral curves with different analytical approaches [1]

Behavioral curves can be caused by two types of loading in a model or structural member:

- 1- Uniform static loading
- 2- Cyclic dynamic loading

In cyclic loading, due to the effects of fatigue due to reciprocating loading and residual stresses, the backbone curves or extremes obtained from the response in each loading cycle, as in Figure 3, generally record less stiffness and strength.

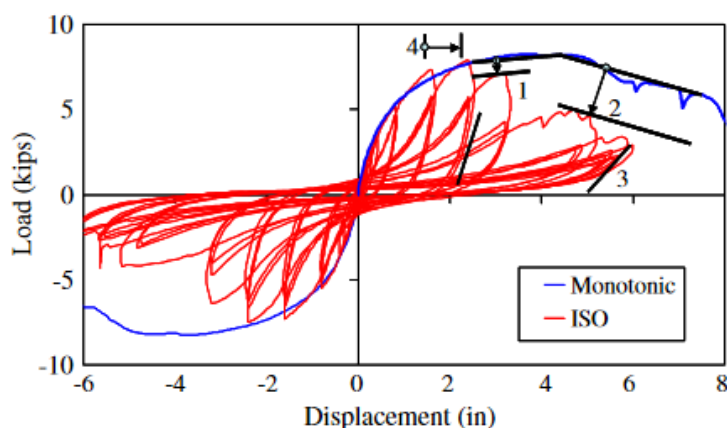


Fig 3: Comparison of behavioral curves with uniform loading and hysteresis loading on a 3ply wood[2]

The first nonlinear model was proposed by Clough and Johnson, including a linear element and an element with a fully plastic elastic behavior [3]. In this model, the deformation of the element depended on the anchor created at both ends. Al-Haddad and White modified the model by changing the location of the plastic joints [6].

In this paper, the aim is to understand the differences in the response of structures according to the type of concentrated or distributed approach, which is followed by the necessary discussions and studies according to the research method.

## Methodology

In this research, using 4 side structural frames taken from the 3D model in Figure (4), the plan of which is taken from the reference [7] with two bays of 5 meters on both sides and three middle bays of 7 meters in the middle of the frame. After designing and analyzing the moment frames based on the tenth topic of the National Building Regulations of Iran (INBR10) and standard 2800 of Iran in ETABS software based on the gravitational load in table (1) and the load combinations in table (2), And its designed sections according to Table (3), they are modeled in OpenSys software, with each of the available approaches for nonlinear modeling of structural members, both concentrated or distributed, ready for the next stages of research. In order to model the mentioned frames in OpenSys software, first the each nodes with the coordinates related to the beginning and end of beams and columns were introduced to the software. These points, as mentioned, will behave in a two-dimensional coordinations with three degrees of freedom, including two degrees of transition and one degree of rotation.

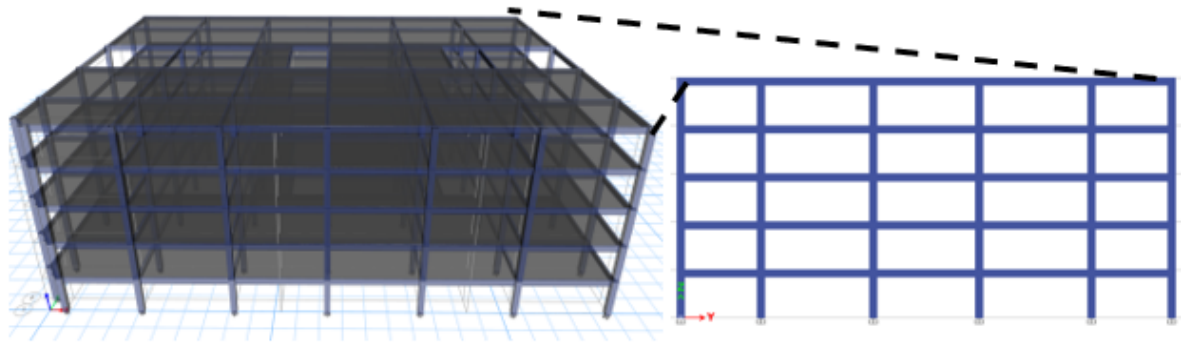


Fig 4:Location of the two-dimensional frame studied in the three-dimensional model of the structure

Table 1:Load rate of models

Load type	Dead load	Live load
Floor + slab	500 kg/m <sup>2</sup>	200 kg/m <sup>2</sup>

Table 2:Analysis and loading details

Design method	LRFD
Load combinations	$1.4 D$ $1.25 D + 1.5 L$ $D + 1.2 L + 1.2 E$ $0.85 D + 1.2 E$

Table 3:Sections of Designed models

SMF-5			IMF-5		
Floors	Column	Beam	Floors	Column	Beam
1-5	BOX 450*450*20	IPE 400	1-5	BOX 450*450*15	IPE 450
SMF-10			IMF-10		
Floors	Column	Beam	Floors	Column	Beam
1-5	BOX 450*450*25	IPE 550	1-5	BOX 450*450*20	IPE 550
6-10	BOX 400*400*20	IPE 400	6-10	BOX 400*400*15	IPE 450

Modeling will be while modeling distributed plasticity with fiber element and modeling concentrated plasticity using zerolength flexural springs at both ends of the beam or column and since the structural members have become two end springs and the middle member in the centralized plasticity approach The energy absorption is not the same in the two parts, so modifications must be made to several arrays of the stiffness matrix of each member, for which a “modellasticbeam2d” member has been used for structural members between plastic joints [8]. This member changes the stiffness matrix at any time by changing the arrays of the stiffness matrix corresponding to each member and considering the degree of division of the total stiffness of each member between the plastic joints and the middle member [9]. Updates the load according to the members' behavioral curve. Considering the ratio of 10 for the stiffness of the end springs to the middle member in the modeled initial frames, finally different ratios are considered to combine the share of each part of the total stiffness of the member, so that the effect of this issue can be investigated in the modeling type.

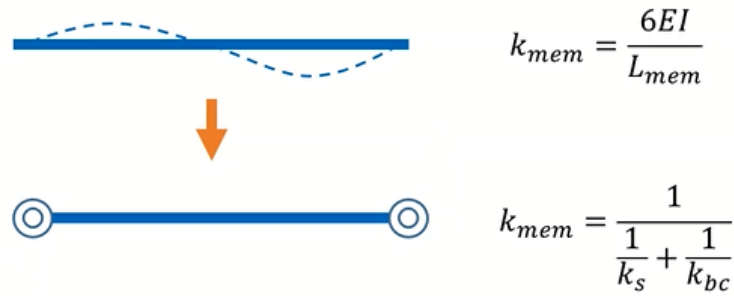


Fig 5: Convert each member to a serial springs

In order to model the behavior of a node with a coordinate in reality in the connection springs as seen in Nodes 3, 4 and 9 in Figure 6, the shear and axial springs are rigid so that for example the forces in each connection spring are properly from the beam Moved to the column and not absorbed. The moment-rotation curve mentioned in Figure 8 is based on uniform loading, and since the hysteric curve of each member has the cross-sectional geometric characteristics and even the amount and type of loading in the structural model [10], the effect of cyclic decay modes of dynamic earthquake loads by The parameter “ $\Lambda$ ” and with bilin material is responsible for converting the behavior curve with uniform loading by changing the maximum resistance and the loading resistance to a curve with dynamic cyclic loading such as earthquake to finally the behavioral curve of the members Approach to cyclic in Figure 7. [11,12]

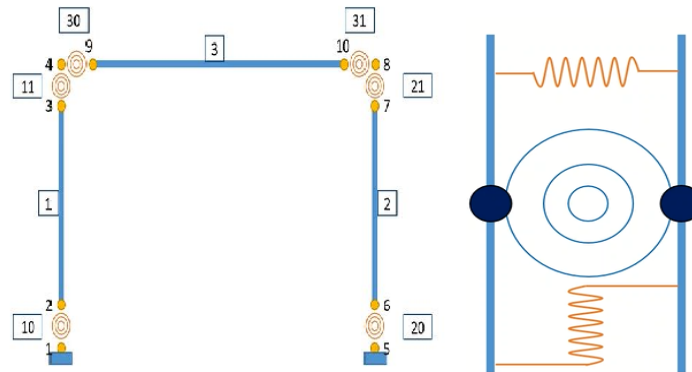


Fig 6: Overview of Zerolength springs and their placement in a single bay moment frame

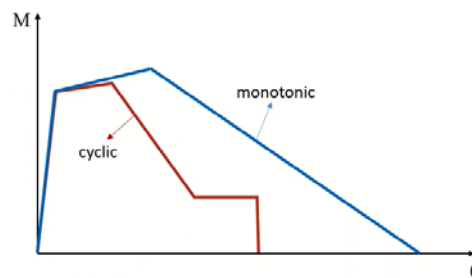
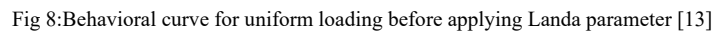


Fig 7: Backbone curve due to uniform and cyclic loading



**considering P- $\Delta$  on the models**

Using selected records from the FEMA-P695 guideline for type D soil in the NEHRP classification according to Table (4), selecting the first earthquake record and its first scale (one tenth more per step) begins the incremental dynamic analysis of the introduced frame. The movements of the frame are recorded by the uniform excitation pattern of its base and the maximum amount of displacement of the frame classes and the acceleration of the corresponding spectrum are recorded as the representative point of this scale from each record and along with the frame response in other scales. The class displacement reaches the limit in the drift criteria, then the algorithm is repeated for each record and the IDA diagrams of each record can be drawn.

Table 4:Used records

No	Earthquake			Station data			
	Name	Station	Magnitude	VS_30(m/s)	PGA(g)	site-source dist	Field distance
1	Northridge	Beverly Hills	6.7	356	0.52	17.2	Far Field
2	Northridge	Canyon Country-WLC	6.7	309	0.48	12.4	Far Field
3	Duzce	Turkey Bolu	7.1	326	0.82	12	Far Field
4	Imperial Valley	Bonds	6.5	223	0.76	2.7	Near Field
5	Imperial Valley	Delta	6.5	275	0.35	22	Far Field
6	Imperial Valley	El Centro	6.5	196	0.38	12.5	Far Field
7	Imperial Valley	Chihuahua	6.5	275	0.28	7.3	Near Field
8	Kobe	Shin-Osaka	6.9	256	0.24	19.2	Far Field
9	Kocaeli	Duzce	7.5	276	0.36	15.4	Far Field
10	Northridge	Saticoy	6.7	281	0.42	12.1	Near Field
11	Landers	Yermo Fire	7.3	354	0.24	23.6	Far Field
12	Landers	Coolwater SCE	7.3	271	0.42	19.7	Far Field
13	Loma Prieta	Capitola	6.9	289	0.53	15.2	Far Field
14	Loma Prieta	Gilroy	6.9	350	0.56	12.8	Far Field
15	Kocaeli, Turkey	Yarimca	7.5	297	0.31	4.8	Near Field
16	Superstition Hills	El Centro	6.5	192	0.36	18.2	Far Field
17	Superstition Hills	Poe Road	6.5	208	0.45	11.2	Far Field
18	Cape Mendocino	Rio	7	312	0.55	14.3	Far Field
19	Chi-Chi	CHY101	7.6	259	0.44	10	Far Field
20	San Fernando	Hollywood Stor	6.6	316	0.21	22.8	Far Field

The transfer method is used to determine how the constraint equations are applied in each analysis. In this method, the equations find a relationship between different degrees of freedom. The equation counter and degrees of freedom are RCM type which uses the Reverse Cuthill Mckee algorithm. Slowly Storage and solution of the system of equations is SPARCE GENERAL type, which uses the Newmark algorithm with parameters  $\beta$  and  $\gamma$ , respectively 0.25 and 0.5. The convergence algorithm is Broyden, and the convergence test is performed through the displacement development instruction with an accuracy of  $10^{-5}$ .

It should be noted that the type of plasticity approach for each frame used in this research is listed in Table (5). In this table, all the frames used are in the form XXX-X-XX, the first three letters representing the intermediate or special ductility, the middle letter indicates the number of stories and the last two letters indicate the type of approach to modeling the plasticity of members, whether distributed (SP) or concentrated (CO).

Table 5: Abbreviations for the used models

Model Name	
IMF-5-CO	IMF-5-SP
IMF-10-CO	IMF-10-SP
SMF-5-CO	SMF-5-SP
SMF-10-CO	SMF-10-SP

In addition, the IMF-5-CO frame has been measured in different classes of stiffness ratio applied to the end springs to the middle member so that the type of structural response in different classes can be measured.

For initial comparison and also verification, through pushover analysis, the response of the intermediate 5 story moment frame in OPENSEES and ETABS software was obtained. This comparison was performed in 3 steps as follows:

1. Nonlinear static response of the whole three-dimensional model in ETABS software and in the north-south direction
2. Nonlinear static response of the studied two-dimensional frame in ETABS software
3. Nonlinear static response of the two-dimensional frame studied in OPENSEES software

The loading pattern of dividing the base shear according to the weight of the floors has been done to push the models by 27 cm. The result of this comparison can be seen for all 3 steps mentioned in Figure 10, also comparing the last two steps separately in Figure 11. A more detailed comparison of these two steps has been drawn. As can be seen, the response of the structure in the two-dimensional frames is close to each other and there is a high difference in the three-dimensional frame. The stiffness of the structure in the lateral direction will be approximately 7 to 8 times bigger from the stiffness of a frame so This high difference in the surface area below the diagram of the 3D model push curves and the 2D frame seems reasonable. Among the two-dimensional frames according to Figure 11 in the range of linear behavior, the difference is very small and in the range of nonlinear behavior the maximum difference is about 12% can be due to differences in the definition of nonlinear parameters in the two software. Therefore, the accuracy of modeling of moment frames in two softwares is acceptable and has a good match with structural concepts.

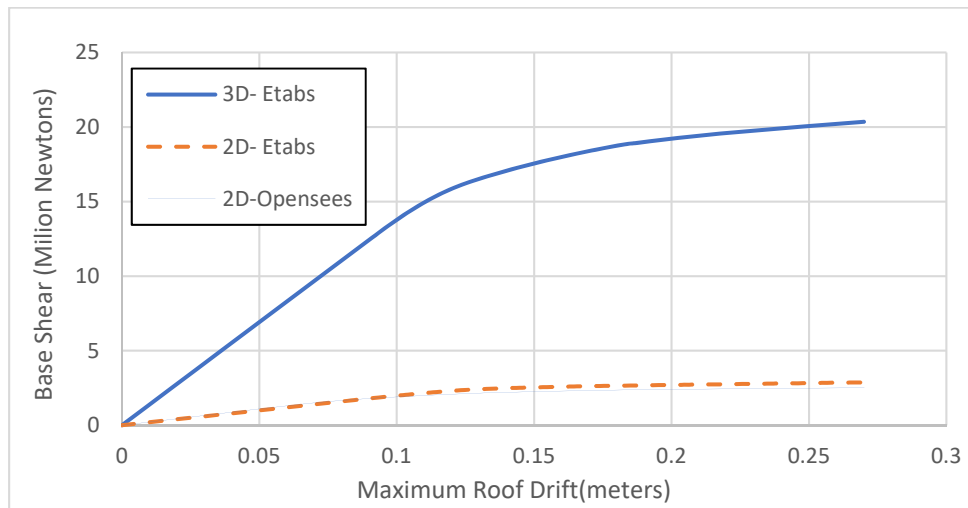


Fig 10: Comparison of push curves of three- and two-dimensional models

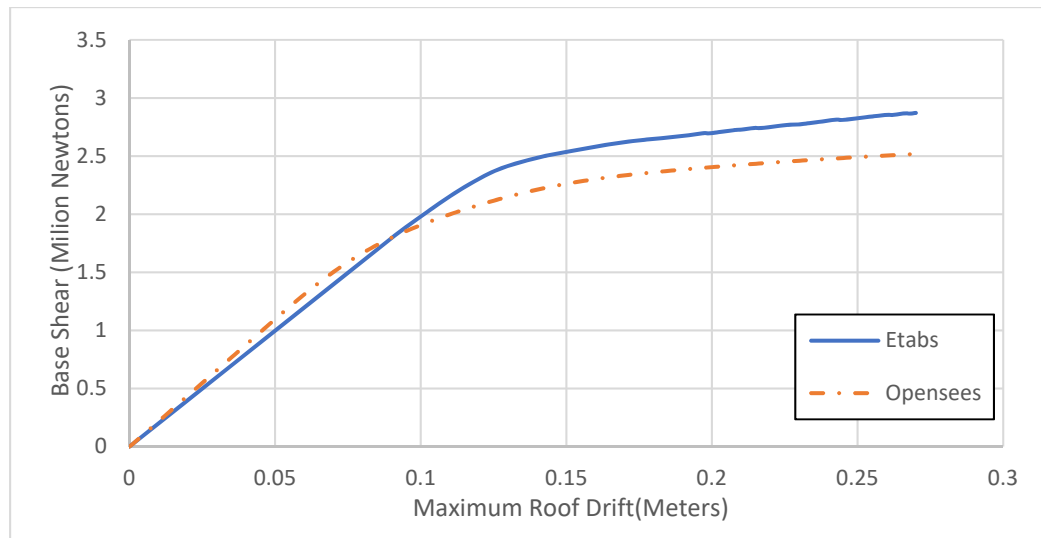


Fig 11: Comparison of the cover curve of two-dimensional models

In addition, a comparison of the nonlinear static response of the structure was performed in two approaches of concentrated and distributed plasticity in OPENSEES software. The results can be seen in Fig 12 and report results with a maximum error of 11%.

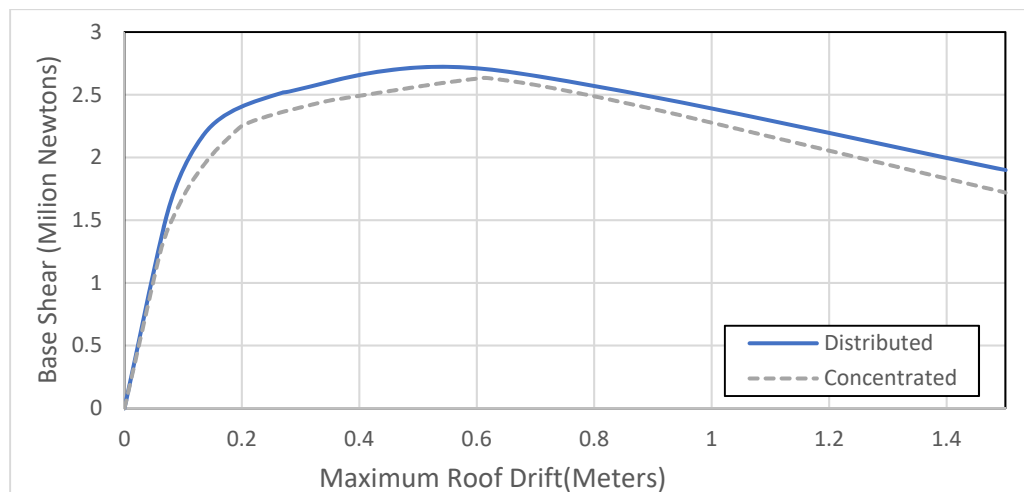


Fig 12: push curve of the two-dimensional models with each approach

### Results of incremental dynamic analysis

The results of IDA analysis obtained from this method along with 16,50,84% percentiles and the function of Log-Normal Density for IMF-5-CO and SMF-5-CO frames are plotted in Figure 13, in addition to the points due to reduction Hardness relative to 20% of the elastic stiffness of each diagram is selected for further investigation in these diagrams. To compare the response of incremental dynamic analysis, 50% percentile curve of each analysis has been used.



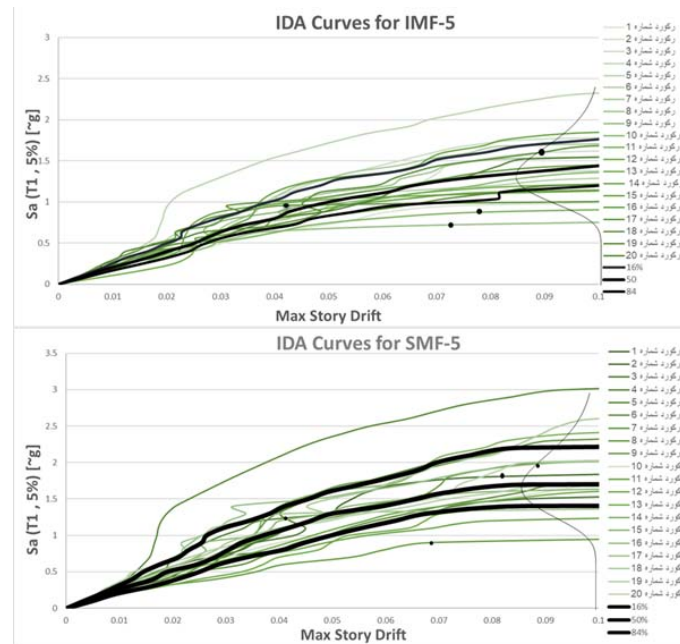


Fig 13: IMF-5-CO and SMF-5-CO IDA curves respectively

In the case of the final performance level of the collapse threshold, we will see a significant reduction in the stiffness and strength of the lateral-resistant force system, a large lateral displacement in the structure. Accordingly, in FEMA350, in moment frames, this limit is set for the IDA curve equal to 20% of the initial elastic slope or  $\theta_{max} = 10\%$ . [16] Therefore, the IDA curves are finally drawn to the drift between the maximum 10%. Has been. The difference in response obtained at this drift level for the 50th percentile of IDA curves is shown in Table (6) as shown in Figure 14 [17,18].

Table 6: Comparison of the spectral acceleration ratio in drift 10% and intersection of curves

Frame	Sa ratio	Intersection
IMF-5	1.06	0.04
IMF-10	1.04	0.06
SMF-5	1.06	0.03
SMF-10	1.01	0.07

Table (6) shows that the design with distributed approach has been able to use more than 8% of the structural capacity, which has been less in more ductile frames, on the other hand, since the difference starts from the time the first member enters to nonlinear range. And in the frames under study, IDA curve in frames with distributed approach with a slight difference at first lower than frames with concentrated approach, more ductile frames such as special and higher frames, intersection and the beginning of the presence of the curve of distributed frames occur later than concentrated frame curves. The noteworthy point in this case is the approximately uniform response of SMF-10 frames with 99% accuracy relative to each other in drifts larger than the intersection point, which is due to the high ductility of this frame. This is because the extension of the plastic joint length in the mentioned frame in the range of drifts that is under study and the type of force redistribution is smaller than other frames when entering the nonlinear area.

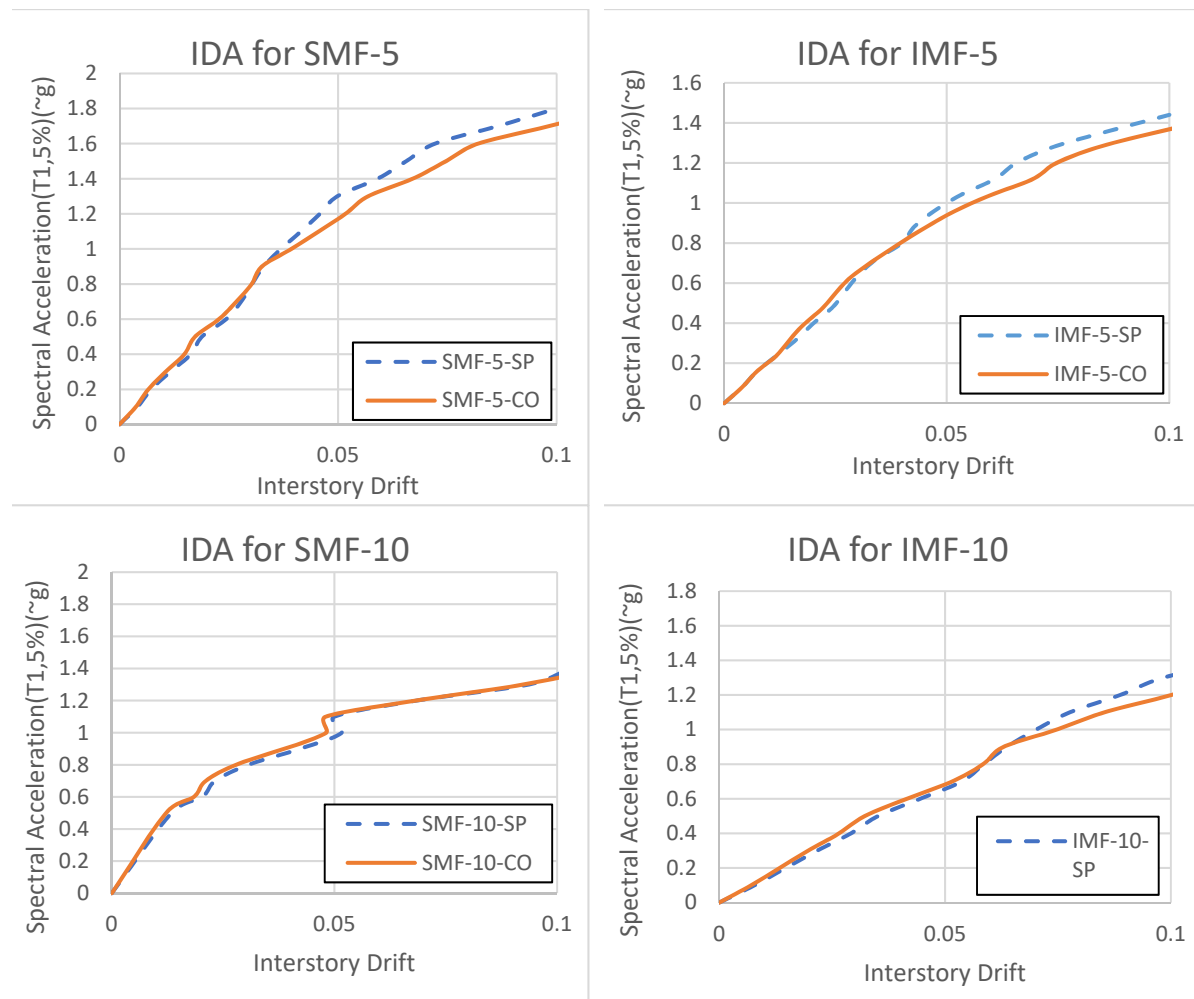


Fig 14: Comparison of 50% percentile in IDA curve of each frame using different plasticity approach

If different stiffness ratios are used for the end springs to the middle member, for each stiffness ratio, the frames record a different period, in which case the final stiffness of the series springs per member remains constant. For example, in Figure 15, the periodicity obtained for different stiffness ratios is plotted on a semi-logarithmic scale for the IMF-5-CO frame, indicating that for stiffness ratios greater than 100 or less than 0.01. The periodicity does not differ significantly from the change in stiffness ratios.

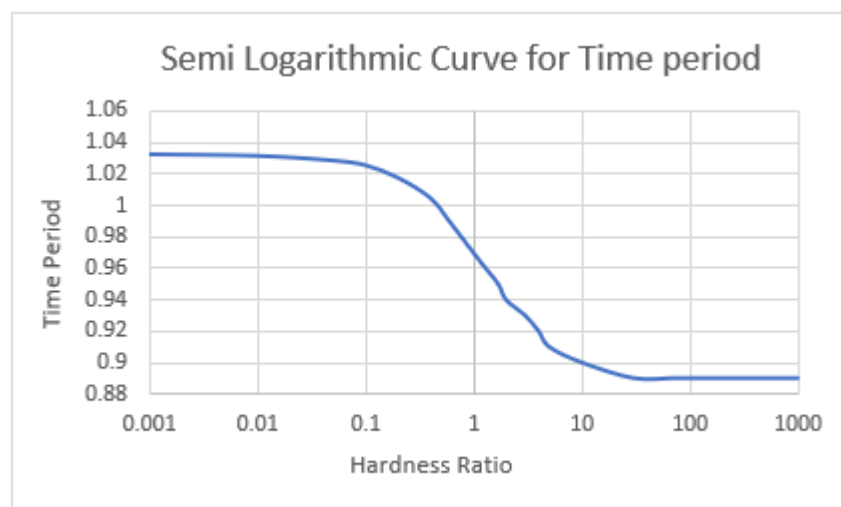


Fig 15: Periodicity change curve for different stiffness ratios of springs to middle member

In the next step, to deepen the mentioned effect, the corresponding spectral acceleration of drift 10% for different stiffness ratios is plotted in Figure (16), the amount of this spectral acceleration in the frame is comparable to the broad plasticity approach.

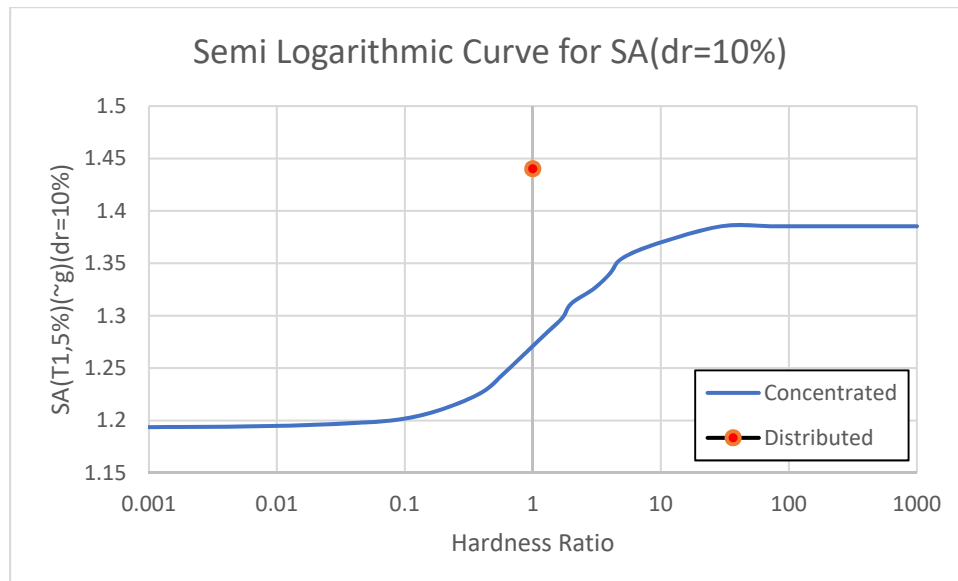


Fig 16: Spectral acceleration corresponding to the collapse threshold for different stiffness ratios

Figure (16) shows that for the frame for different hardness ratios, the spectral acceleration corresponding to the collapse threshold is different and increases with increasing stiffness ratio. On the other hand, considering the above-mentioned figure, since the curve does not change much for hardness ratios higher than 100 or less than 0.01, by comparing the spectral acceleration of the collapse threshold in the case of distributed plasticity approach, it can be said that The reason for the redistribution effect of this plasticity approach, capacity of the frame in all cases is more than the case of concentrated plasticity.

## Results

- Considering the nonlinear behavior of materials has a significant effect on the structural response. This effect is more visible in dynamic analysis. Concentrated and distributed plasticity methods are widely used to model the nonlinear behavior of materials. In this study, nonlinear static analysis and incremental dynamic analysis of 4 steel moment frames were performed considering the behavior of concentrated and distributed plasticity. The results of these modelings show that the approaches considered for modeling the nonlinear behavior of steel elements have an almost similar response in terms of maximum response structural drift. In general, the spectral acceleration ratio of the collapse threshold in the two approaches is 1 to 6%, which is less in more ductile frames as the intersection of the two IDA curves occurs in larger drifts.
- In the next step, to deepen the results for one of the frames modeled with concentrated springs, free dynamic vibration analysis was performed for different stiffness ratios between the end springs and their middle member. The results show that by increasing the stiffness ratio in While the total stiffness remains constant, the periodicity decreases in the range of 0.01 to 100 and the spectral acceleration of the collapse threshold increases and remains constant for other values. It was also found that the collapse capacity in the modeling mode with a distributed approach will be shown more than in all hardness cases in modeling frames with a concentrated approach.

## References

- [1] Huu-Tai Thait al. Review of nonlinear analysis and modelling of steel and composite structures, International Journal of Structural Stability and Dynamics, 2020
- [2] Ibarra LF, Medina RA, Krawinkler H. Hysteretic models that incorporate strength and stiffness deterioration. Earthquake engineering & structural dynamics. 2005
- [3] Clough RW, Johnston SB "Effect of stiffness degradation on earthquake ductility Requirements", In Transactions of Japan earthquake engineering symposium, Tokyo, pp. 195–8, 1966.
- [4] Giberson MF, "The response of nonlinear multi-story structures subjected to earthquake excitation", Ph.D. Dissertation, California Institute of Technology, Pasadena, CA, 1976.
- [5] Giberson MF, "Two nonlinear beams with definitions of ductility", J Struct Div, Vol. 95(2), 1969
- [6] Spacone E, Filippou FC, Taucer FF, "Fibre beam–column model for non-linear analysis of RC frames: Part I: Formulation", Earthquake Engineering and Structural Dynamics, Vol. 25, pp. 711–725, 1996.
- [7] Hinduabadi, R. ,, Probabilistic analysis of seismic performance of hospitals. Thesis of Tarbiat Modares University, 2017

- [8] Zareian, Farzin, and Ricardo A. Medina. "A practical method for proper modeling of structural damping in inelastic plane structural systems." *Computers & structures* 2010: 45-53.
- [9] Zareian, Farzin, and Helmut Krawinkler. *Simplified Performance-Based Earthquake Engineering*. , 2006.
- [10] Ibarra LF, Medina RA, Krawinkler H. Hysteretic models that incorporate strength and stiffness deterioration. *Earthquake engineering & structural dynamics*. 2005 Oct;34(12):1489-511.
- [11] Lignos DG, Hartloper AR, Elkady A, Deierlein GG, Hamburger R. Proposed updates to the ASCE 41 nonlinear modeling parameters for wide-flange steel columns in support of performance-based seismic engineering. *Journal of Structural Engineering*. 2019 Sep 1;145(9):04019083.
- [12] NIST, "Guidelines for Nonlinear Structural Analysis for Design of Buildings", Report no.2017b
- [13] Lignos DG, Krawinkler H. "Sidesway collapse of deteriorating structural systems under seismic excitations." Rep. No. TR 172, John A. Blume Earthquake Engineering Research Center. 2009.
- [14] H. Krawinkler, F. Zareian, D. G. Lignos, and L. F. Ibarra, "Prediction of collapse of structures under earthquake excitations," in *Proceedings of the 2nd International Conference on Computational Methods in Structural Dynamics and Earthquake Engineering (COMPDYN 2009)*, Rhodes, Greece, CD-ROM paper, paper no. CD449, 2009, pp. 22-24.
- [15] Ibarra, LF and Krawinkler, H.. *Global Collapse of Frame Structures under Seismic Excitations*. John A. Blume Earthquake Engineering Center Technical Report 152. Stanford Digital Repository, 2005.
- [16] Federal Emergency Management Agency, "Recommended Seismic Design Criteria for New Steel Moment-Frame Buildings". Report No. FEMA-350, Federal Emergency Management Agency, Washington, DC, 2000.
- [17] Vamvatsikos, D. and Cornell, C.A. "Incremental Dynamic Analysis. s.l.": *Earthquake Engineering and Structural Dynamics*, pp. 491-514, 2002
- [18] Vamvatsikos, Dimitrios & Cornell, C. *The incremental dynamic analysis and its application to performance-based earthquake engineering*. 2002.