Design of an Overhead Tank for the Newly Built Guest House in Cit (Central Institute of Technology, Assam)

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Abstract-An investigation was carried out to study the various losses of head in circular pipes. This was done in order to check the feasibility to design a tank for the guest house building for supplying water for domestic purposes in the building. Considering three peak times of water usage i.e. morning 7-9 am, afternoon 12-2 pm and evening 6-8 pm and assuming a certain number of plumbing fixtures to be in use at the same time, an effort was made to calculate the feasibility of the overhead tank. And after investigation this was found that the total head required for the overhead tank to be 18 m. So a pump of 4.5 hp was proposed. Moreover as per analysis, it has been found and thus advisable to install an overhead tank of dimension (5×2.5) m² to meet the water requirements of the newly built guest house. And this requirement was found to be compatible in all the conditions those have been considered.

Key words: Head loss; flow in pipes; Discharge; Losses in pipes.

List of Symbols and Abbreviation

Symbol Description

D	Diameter
V	Velocity
ρ	Density

- A Cross-sectional area
- Q Discharge
- Re Reynolds number
- f Co-efficient of friction
- h_f Head loss due to friction
- f' Frictional resistance
- θ Angle of elevation
- w Specific weight
- p Pressure
- H Head
- g Specific gravity
- Z Potential head

HGL Hydraulic Gradient Line

INTRODUCTION

I.

New Guest House is constructed in CIT (Central Institute of Technology, ASSAM) Campus to serve the guest of the CIT. It is situated beside the Teachers Quarter and to the east of Balagaon Transit Boys Hostel. The main objective of the analysis was to design an overhead tank with required head to supply water to the guest house building by calculating different head losses in pipes, assuming a certain number of plumbing fixtures to be in use at the same time. A pipe is a closed conduit which is used for carrying fluids under pressure. Pipes are commonly circular in section. As the pipe carry fluids under pressure, the pipes always run full. The fluid flowing in the pipes is always subjected to resistance due to shear forces between fluid particles and the boundary walls of the pipe and between the fluid particles themselves resulting from the viscosity of the fluid [1]. The resistance to the flow of the fluid is in general known as frictional resistance. Since certain amount of energy possessed by the flowing fluid will be consumed in overcoming this resistance to the flow, there will always be some loss of energy in the direction of flow, which however depends on the type of flow. The flow of the liquid in the pipe may be laminar, turbulent, or in a state of transition depending upon Reynolds number of flow [2-9].

However, turbulent flow can be very complex one that as yet has been defined a rigorous theoretical treatment. Since different laws govern these two types of flow in pipes, the same are required to be dealt separately. Moreover, the introduction of different diameters of pipes leads to the losses due to contraction or expansion of the pipes. Also the change in the gradient, if any, contributes to the overall losses of head [10-12].

II. LOSSES IN PIPE FLOW

a. Head Loss

Certain amount of energy proceed by the flowing fluid will be consumed in overcoming the frictional resistance of the flow, there will always be some loss of energy in the direction of flow. This energy loss results in reduction of head of the fluid and hence termed as head loss and can be classified as [15]:

b. Major Losses

The loss of head or energy due to friction in a pipe is known as major loss. As fluid flow through a pipe, resistance are experienced which results in reduction of velocity and ultimately the head. The friction being the predominant loss is of main concern. Head loss in pipes due to friction can be calculated using Darcy's Weisbach equation [16].

Loss of head (or energy) due to friction: Darcy-Weisbach equation

Considering a pipe having a cross-sectional area A carrying a fluid with a mean velocity V.

Let 1 and 2 be the two sections of the pipe, L distance apart. Let the intensities of the pressure be P_1 and P_2 respectively. By applying Bernoulli's equation between the sections 1 and 2, we obtain

$$\frac{P_1}{w} + \frac{V^2 1}{2g} + Z_1 = \frac{P_2}{w} + \frac{V^2 2}{2g} + Z_2 + h_f$$

Since $V_1 = V_2 = V$ and $Z_1 = Z_2$

Loss of head = $h_f = (p_1/w) - (p_2/w)$

i.e., the pressure intensity will be reduced by the frictional resistance in the direction of flow and the difference of pressure heads between any two sections is equal to the loss of head due to friction between these sections.

Further let f' be the frictional resistance per unit area at unit velocity, then the frictional resistance

 $= f' \times area \times V^n$

 $= f' \times PL \times V^n$

Where P is the wetted perimeter of the pipe.

The pressure forces at the sections 1 and 2 are (p_1A) and (p_2A) respectively.

Thus resolving all the forces horizontally, we get

 $P_1A = p_2A +$ frictional resistance

Dividing both sides by the specific weight 'w' of the flowing fluid, we get

$$\frac{p_1 - p_1}{w} = \frac{f'}{w} \times \frac{P}{A} LV^2$$

$$h_f = \frac{p_1 - p_2}{w} \quad \text{then}$$

$$h_f = \frac{f'}{w} \times \frac{P}{A} \times LV^n$$

The ratio of the cross-sectional area of the flow (wetted area) to the perimeter in contact with the fluid (wetted perimeter) i.e. (A/P) is called hydraulic mean depth (H.M.D) or hydraulic radius and it is represented by 'm' or 'R'.

Then $h_f = (f'/w) \times (L V^n)$ For pipes running full,

 $-p^2/4$

$$m = \frac{A}{V} = \frac{\pi D^2/4}{\pi D} = \frac{D}{4}$$

Substituting this in the equation for h_f and assuming n = 2,

$$h_f = \frac{4f'}{w} \times \frac{LV^2}{D}$$

Putting
$$\frac{4f'}{w} = \frac{f}{2g}$$

 $h_f = \frac{fLV^2}{2gD}$ (i)

Where fis known as friction factor or co-efficient of friction, which is a dimensionless quantity.

The equation (i) is known as Darcy Weisbachequation which is commonly used for computing the loss of head due to friction in pipes. It may be noted that the head loss due to friction is also expressed in terms of velocity head $(V^2/2g)$ corresponding to the mean velocity [13, 14]. Further the observation shows that the coefficient 'f' is not constant but its value depends on the roughness condition of the pipe surface and the Reynolds' number of the flow. As such, in order to determine the loss of head due to friction correctly, it is essential to estimate the value of f correctly. For this purpose, on the basis of experimental observations the value have being developed, which indicate the manner in that f varies and also facilitate the correct estimation of the value of the friction factor f [5.a].

Hazen William's formula:

It is a formula which is widely used for designing water supply systems. According to this formula the mean velocity of flow is given by

$$V = 0.85 C_1 R^{0.63} S^{0.54}$$

Where C_1 is the co-efficient, the value of which depends on the value of boundary. Some of the value of C_1 is given below:

Sl. No	Type of pipe	Value of C ₁
1	Extremely smooth and straight	140
2	Very smooth	130
3	Smooth wood stove, smooth masonry	120
4	New riveted steel	110
5	Old riveted steel	95

TABLE 1. Values of C1

c. Hydraulic Gradient Line (H.G.L)

It is defined as the line which gives the sum of pressure head $\left(\frac{p}{w}\right)$ and datum head (z)of a flowing fluid in a pipe with respect to some reference line or it is the line which is obtained by joining the top of all vertical ordinates, showing the pressure head (p/w) of a flowing fluid in a pipe from the center of the pipe [5.b].

The following points are worth noting:

- (1) Energy gradient line (E.G.L) always drops in the direction of flow because of loss of head.
- (2) Hydraulic gradient line (H.G.L) may rise or fall depending upon the pressure changes.
- (3) Hydraulic gradient line is always below the energy gradient line (E.G.L) and the vertical intercept between the two is equal to the velocity head $(V^2/2g)$.
- (4) For a pipe of uniform cross-section the slope of the hydraulic gradient line is equal to the slope of the energy gradient line.

(5) There is no relation whatsoever between the slope of energy gradient line and the slope of the axis of the pipe.

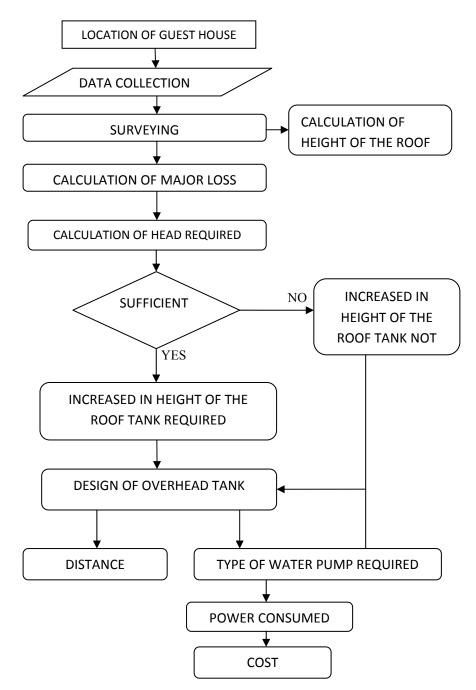


Fig.1.Flow chart of the activities of the study

III. DESCRIPTIONS

For the prosecution of analysis some data that cannot be practically known or calculated were required. For that reason these data's from different organizations, person or team concerned were enquired from Kokrajhar town. Various data's that are collected from different organization are tabulated below:

TABLE 2. C	ollected data
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DATA COLLECTED	ORGANIZATION
Plan of the guest house building	Contractor
Minimum head for different plumbing fixtures	Hardware Shop, Kokrajhar
Electrical Ratings	Kokrajhar power house
Rate of Pumps	Hardware Shop, Kokrajhar

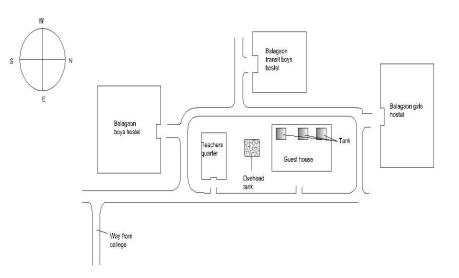


Fig. 2. Topography of the area under observation

Surveying

Measurement of the building (guest house, CIT) $\Theta_1 = 13^\circ 23' 5''$ $\Theta_2 = 1^\circ 43' 33''$

OC = 31.25 mHeight of the tank = $31.25(\tan\Theta_1 + \tan\Theta_2)$

= 8.38 m

TABLE 3. Measurement of Tank Height

T AT	T0		FACE:LEFT								FACE:RIGHT								AVERAGE VERTICAL ANGLE							
INSTRUMENT	SIGHTED		С		Ι)	Ν	MEAN	1		RTIC NGL			A		E	3	N	MEAN	1		RTIC NGL				
INS	S	0	,		,	,,	o	,	••	o	,	••	0	,	· ·	•	,,	0	,	· ·	o	,	···	o	,	• •
0	А	1	4 4	5	4 3	10	1	43	37	1	43	37	1	4 4	00	43	0 0	1	4 3	30	1	4 3	30	1	4 3	3 3
	С	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	В	1 3	2 3	1 0	2 3	50	13	23	10	13	23	10	1 3	2 3	00	23	0 0	13	2 3	00	13	2 3	00	13	2 3	5

In S.I. units, the unit of viscosity is used as discussed below:

1 poise = 0.0102 kg-sec/m²

 $= 0.0102 \times 9.81$

 $= 0.1 \text{ N-sec/m}^2$

IV. RESULTS AND DISCUSSIONS

A. Effect of Temperature on Viscosity

The following table gives the values of viscosity of water at different temperatures [1].

Temperature of	Coefficient of viscosity (µ	L)
water in °C	in kg-sec/m2	in poise
0	$183.2 \times 10-6$	0.01780
5	151.7 × 10-6	0.01518
10	133.2 × 10-6	0.01310
20	102.3 × 10-6	0.01009
30	81.80 × 10-6	0.00804
40	66.50 × 10-6	0.00654
	47.90 × 10-6	0.00478
60	36.30 × 10-6	0.00366
80	$28.80 \times 10-6$	0.00295
100		

TABLE 4. Viscosity at different temperature

TABLE 5. Practical Calculation for Major Losses

A (Area)	G (gravity)	ρ_m (density of manometer)	ρ _w (density of water)	d (dia. of pipe)	L (length)
0.77 m ²	9.81 m/sec ²	136000 kg/m ³	1000kg/m ³	0.022 m (For pipe ³ / ₄ ") 0.016 m(For pipe ¹ / ₂ ")	1.25 m (For ³ /4" pipe) 1 m (For ¹ /2" pipe)

TABLE 6. Observation data for larger pipe

S.No	h1, cm	h2, cm	R1, cm	R2, cm	t, sec
1	15.5	12.4	6.20	6.8	13.62
2	15.5	12.4	18.1	5.4	12.95
3	15.5	12.4	23.9	9.8	15.06
AVERAGES	15.5	12.4	16.07	7.33	13.88

Calculations

R = R1 - R2/100	= 0.087 m
$Q = A \times R/t$	$= 4.83 \times 10^{-4} \text{ m}^{3}/\text{sec}$
$a = \pi d^2/4$	$= 3.80 \times 10^{-4} \text{ m}^2$
V = Q/a	= 1.27 m/sec
$h = h_1 - h_2/100$	= 0.031 m
$f = h_f 2gd / (4LV^2)$	= 0.02
$h_{\rm f} = h ((\rho m / \rho_{\rm w}) - 1)$	= 0.39 m
Theoretical calculation fo	r larger pipe:
Temperature	= 27.8° C
ρ	= 996.4
V _{act}	= 1.27 m/sec (Taken from practical)
Re	$= \rho v d/\mu$
	$= 0.32 \times 10^5$
f	$= 0.079/\text{Re}^{1/4}$
	$= 5.89 \times 10^{-3}$
$h_{\rm f}$	$=4 \mathrm{f} \mathrm{LV}^2 / (2\mathrm{gD})$
	= 0.11 m

	SlNo	h1, cm	h2, cm	R1, cm	R2, cm	t, sec
	1	18.4	9.5	16.7	8	9.56
	2	18.4	9.5	19.1	9.8	10.19
	3	18.4	9.5	28	9.4	21.37
AV	VERAGES	18.4	9.5	21.27	9.06	13.71

TABLE 7.Observation data for smaller pipe

= 0.122 m R = R1 - R2/100 $= 6.852 \times 10^{-4} \text{ m}^{3}/\text{sec}$ $O = A \times R/t$ $= 2.012 \times 10^{-4} \text{ m}^2$ $a = \pi d^2/4$ V = Q/a= 3.406 m/sec $h = h_1 - h_2/100$ = 0.089 m $f = h_f 2gd / (4LV^2)$ = 0.026 $h_{f} = h ((\rho m / \rho_{w}) - 1)$ = 1.12 mTheoretical calculation for smaller pipe: Temperature $= 27.8^{\circ} \text{ C}$ = 996.4ρ Vact = 3.406 m/sec (Taken from practical) $= \rho v d/\mu$ Re $= 0.64 \times 10^{5}$ $= 0.079/\text{Re}^{1/4}$ f $=4.97 \times 10^{-3}$ $= 4 f LV^2 / (2gD)$ $h_{\rm f}$ = 0.73 m

Calculation of losses due to friction for guest house

Assuming the tank outlet to be a mouthpiece, actual velocity of the water at the exit is calculated by the formula-Vact $=0.855\sqrt{(2gH)}$ Where Depth of the tank (H) = 1.48mCalculation of Reynolds Number $= (\rho v D)/\mu$ Re Where ρ = specific wt. of water; V = velocity of water; D = dia. Of the pipe; μ = dynamic viscosity Calculation of friction factor (f) If Re<2000, f = 16 $= 0.079/(\text{Re})^{1/4}$ 4000<Re<10⁶, f Upto 10^7 , f $= 0.008 + (0.05525/\text{Re}^{0.235})$, for smooth pipes.

Calculation of head loss due to friction $h_f = 4fLV^2/(2gD)$ Power losses to maintain the flow. $P_1 = (\rho gQh_f)/1000$ Q = Discharge = V.AWhere A = Cross-section area $= (1/4)\pi D^2$ Assuming number of plumbing fixtures as shown belowa. Three wash basin b. Three shower

c. Two tap at water closet

d. Three tap at bathroom

Minimum Head at the top of the roof can be calculated from the Table below

Temp of water	4	10	15	21	26	32	37	43	49	65
in deg.c										
Specific weight in kg/m ³	1000	999.72	999	998	997	996	993	991	990	980

TABLE 8. Temperature vs. Specific weight for measuring Head

1. Power required for overcoming residual head (when head loss due to friction > head available)

 $P2 = (\rho g Q h_2) / 1000 \text{ KW}$

Where h_2 = Total pressure residual head for the plumbing fixtures.

TABLE 9.	Total	residual	Head	for	all	plumbing	fixtures
	1000	reoraaaa				promotions	

SL NO	Plumbing Fixtures	No. of fixtures	Residual Head (m)
1	Wash Basin	3	$5.64 \times 3 = 16.92$
2	Shower	3	$8.45 \times 3 = 25.35$
3	1 tap at W.C	2	$3.5 \times 2 = 7$
4	1 tap at Bath room	3	$3.5 \times 3 = 10.5$
		Total = 59.77 or 5.	43/fixtures

Assuming eleven fixtures are used at a time in a house at the peak hour, therefore required head at the top of the roof of the quarters for the above fixtures equal to 59.77/11 i.e. 5.43m per fixtures. Assuming peak hours of flow through plumbing fixtures to the guest house to be 7 AM to 9 AM morning, 12 noon to 2 PM and 7 PM to 9 PM, the values of specific weight and dynamic viscosity will change as per table. Thus the head loss will also be a function of temperature.

Calculations for full tank in morning, afternoon and evening are tabulated below For middle tank ground floor (Here L = 10.78 m)

Table 10. Data's for middle tank, ground floor, morning & evening

$T = 23.8^{\circ}$, Morning & Evening				
V	Q	Re	F	$h_{f}(m)$
(m/s)	(m^{3}/s)			
4.61	0.0042	1.635	3.93	5.55
		$\times 10^5$	$\times 10^{-3}$	

For middle tank first floor (Here L = 2.9 m)

TABLE 12. Data's for middle tank, ground floor, afternoon

$T = 28^{\circ}$, Afternoon				
V	Q	Re	f	$h_{f}(m)$
(m/s)	(m^{3}/s)			
4.61	0.0042	1.799	3.84×10^{-3}	5.42
		$\times 10^5$	10-3	

For middle tank first floor (Here L = 2.9 m)

 TABLE 14. Data's for two side tanks ground floor, morning & evening

T = 23.8°, Morning & Evening				
V	$Q(m^3/s)$	Re	F	$h_{f}(m)$
(m/s)				
4.61	0.0042	1.635	3.93×10^{-3}	7.89
		$\times 10^5$	10-3	

For two side tanks first floor (Here L = 15.34 m)

Table 11.Data's for middle tank, first floor, morning & evening

$T = 23.8^\circ$, Morning & Evening					
V (m	/s)	$Q(m^3/s)$	Re	F	$h_{f}(m)$
4.6	1	0.0042	1.635	3.93 ×	1.49
			$\times 10^5$	10-3	

For middle tank ground floor (Here L = 10.78)

Table 13. Data's for middle tank, first floor, afternoon

$T = 28^{\circ}$, Afternoon				
V (m/s)	Q	Re	F	$h_{f}(m)$
	(m^{3}/s)			
4.61	0.0042	1.799	3.84 ×	1.46
		$\times 10^5$	10-3	

For two side tanks ground floor (Here L =15.34 m)

Table 15. Data's for two side tanks first floor, morning & evening

$T = 23.8^{\circ}$, Morning & Evening				
V (m/s)	$Q (m^3/s)$	Re	F	$h_{f}(m)$
4.61	0.0042	1.635 ×10 ⁵	3.93 × 10 ⁻³	7.89

For two side tanks ground floor (Here L = 15.34 m)

$T = 28^{\circ}$, Afternoon				
V	$Q(m^3/s)$	Re	f	$h_{f}(m)$
(m/s)				
4.61	0.0042	1.799	3.84 ×	7.71
		$\times 10^5$	10-3	

Table 17.	Data's	for two	side tanks	first floor,	afternoon
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$T = 28^{\circ}$, Afternoon				
V (m/s)	$Q(m^3/s)$	Re	f	$h_{f}(m)$
4.61	0.0042	1.799	3.84 ×	7.71
		$\times 10^5$	10-3	

For two side tanks first floor (Here L = 15.34 m)

From the above tables, the average head of guest house = 5.66 m

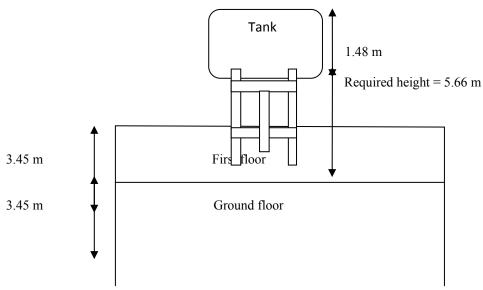


Fig. 4. Height of guest house tank

Therefore total height of guest house tank = (3.45 + 3.45 + 5.66 + 1.48) m = 14.04 m

V. DESIGN OF OVERHEAD TANK

Since, Discharge (Q)	$= 4.20 \times 10^{-3} \text{ m}^3/\text{s}$
	= 4.20 lit/s
Total volume of water required for 2 hrs	$= 2 \times 4.20 \times 60 \times 60$
	= 30240 liters = 31000 liters (approx)
Let, Length (L)	= 2 times of Breadth
Height $(H) = Breadth (B)$	
$L \times B \times H$	= 31000 liters
$2B^3$	$= 31 \text{ m}^3$
Therefore, B	= 2.5 m
L	= 5 m
Н	= 2.5 m
Check: $L \times B \times H$	$= 31.25 \text{ m}^3 \text{ or } 31250 \text{ liters}$
Assuming diameter of pipe = 6 cm	

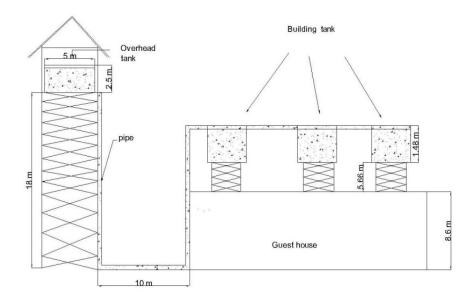
Head loss due to friction for the 10 m length (Here, h = 2.5 m and L = 10 m)

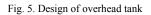
TABLE 18. Head loss due to friction for the 10 m length, TABLE 19. Head loss due to friction for the 10 m length, morning & evening afternoon

$T = 23.8^{\circ}$, Morning & Evening					$T = 28^\circ$, Afternoon				
V (m/s)	$Q(m^3/s)$	Re	F	$h_{f}(m)$	V (m/s)	$Q(m^3/s)$	Re	F	$h_{f}(m)$
5.99	0.0169	3.85×10^{5}	3.17 × 10 ⁻³	3.86	5.99	0.0169	4.24 ×10 ⁵	3.09×10^{-3}	3.77

Therefore maximum head loss due to friction	= 3.86 m								
Therefore the total height of overhead tank	= 14.04 + 3.86								
	= 17.90 m								
	= 18 m (approx)								
Therefore total head of overhead tank should be 18 meters.									
VI. PUMP OPERATING COST									
For 20 m head 1.02 hp pump can lift	= 84 lit/min								
Therefore for 2 hours it can pump	= 10080 liters								
For 31000 liter capacity tank total hp required	= 31000/10080								
	= 3.07 hp								
	= 3 hp (approx)								
Pump rating as 3 hp, assuming 80% efficiency input power is [5.a].									
3.75 HP	= 2.81 KW								
One unit	= 1 KWh								
Cost of 1 unit as per Assam Electricity Board	= Rs 4.20/unit								
If useof the pump is for two hours morning, noon and evening each, total of 6 hrs/day.									
Therefore pump operation cost	$= \operatorname{Rs} \left(6 \times 31 \times 2.81 \times 4.20 \right)$								
U_{are} 21 - no of days in a month									

Here, 31 = no. of days in a month = $D_{c} 2105 17$ / month





VII. CONCLUSION

One of the most typical and common problem faced by the Engineers dealing with pipe flow system is the calculation of required head for a system and measuring the losses of head. According to the Bernoulli's equation the energy and the mass must remain conserved throughout the conveyance of water. But in practical it is not so, because of the various factor causing the head loss in the pipe system. This may be due to frictional forces on the water flowing in the surface of the pipe, or by the fluid itself, may be due to the different shape sizes of the pipe fittings.

In the study consideration was on the major losses because with comparison to it, minor losses such as due to bends in the pipes, sudden contraction or sudden expansion, are very small. Though it can be calculated by measuring equivalent length and further can be added to the overall length of the pipe. Thus, by measuring the head losses and height of the guest house it was concluded that an overhead tank with a height of 18 m

should be designed which can be located at a distance of 10 m form the guest house. Also the height of the guest house tank should be increase more with 5.57 m which will give the required head to supply water with adequate pressure.

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