Design and Manufacturing of Laminated Spring: A New Approach Based On Composites

Rohit Ghosh#1, Sushovan Ghosh#2, Tanuj Srivastava#3, Dr. Rabindra Nath Barman #4

#1,#2 B.Tech student, #3 M.Tech student, #4 Assistant Professor, Department of Mechanical Engineering, National Institute of Technology Durgapur, Durgapur, West Bengal, India, Pin-713209
#1 rohit.99.2016.nitdgpr@gmail.com, #2 sushovanghoshnitdgp@gmail.com #3 tanujsrivastava28@gmail.com, #4 rahul.barman@yahoo.co.in

Abstract---A laminated spring or a leaf spring, being one of the overriding components of an automobile suspension system is nowadays, considered to be a potential factor for reducing vehicle weight. With the advent of composite materials, it has been possible to reduce the weight of the leaf spring without any reduction in the load carrying capacity and stiffness. Composites are well suited for leaf spring applications due to their high strength to weight ratio, fatigue resistance and natural frequency. The achievement of weight reduction with apposite improvement of mechanical properties has made composites an excellent replacement for conventional steels.

The present work is an endeavour to provide the readers as well as the industry with an exclusive construction technique regarding composite leaf springs based on an experimental affirmation. Apart from that, the present work converges itself towards the comparative study of steels and composites for the bending stress evaluation and distribution associated with two different categories of leaves in the new construction method based on the rule of mixtures; which again has been one of the parts of the recent developments cognated with the composite leaf springs. The laminated spring was modeled in CATIA V5R18 and the same were analyzed under similar conditions using ANSYS (Workbench 16.2) software considering Structural-Steel and Carbon fiber Steel as the spring material for respective studies. Finally, software based results are presented and compared for two distinct cases mentioned above.

Key words: Laminated spring; CATIA V5R18; ANSYS (Workbench 16.2); Carbon fiber steel.

I. INTRODUCTION

A spring is an elastic machine element which undergoes deflection for the application of any load and intends to regain its original shape depending upon the magnitude of the applied load. The major applications of spring may include its use as a shock and vibration absorber and storing potential energy by its deflection during the application of load. A multi-leaf spring or laminated spring is a very important component in automobile suspension system. It is one of the oldest suspension components too and still today it is extensively used in all the heavy and light duty commercial vehicles, railway wagons and usually in the rear suspension of passenger vehicles. It differs from the conventional helical spring in a way that it can be guided along a definite path and it deflects under the application of load while acting as a structural member. This concept is employed during the analysis of bending stresses in different leaves by consideration of cantilever beam [1-2]. The present work makes an attempt to validate the above concept by performing static structural analysis using ANSYS software for the evaluation of maximum bending stress and subsequently bending stresses in different leaves, which in all, construct the entire spring. Finally, the reader may get an exposure regarding the bending stress variations for the multi-leaf spring for both the cases associated with steels and composites, which obviously differs from that of any cantilever beam section.

In its construction the leaf spring consists of a series of flat plates or leaves, usually of semi-elliptic shape, which are held together with the help of U-bolts and centre clip. Generally two types of leaves may be observed in a multi-leaf spring i.e. some graduated-length leaves and a few extra full-length leaves. The length of the leaves gradually decreases from top to bottom. The longest leaf in the top is known as master leaf which is bent at both the ends to form spring eyes. The extra full-length leaves are inserted between the master leaf and the graduated-length leaves to support the transverse shear force. In order to maintain proper alignment and to restrict the lateral shifting of leaves, rebound clips are used [3]. In practice, these springs rest on the axle of an automobile. Its front end is connected with the frame by means of a simple pin joint and the rear end is connected with the frame through a flexible link (known as shackle) [4].

A number of research studies have been carried out in this context to replace the conventional materials of the leaf spring by composites to enhance its load carrying capability and to reduce the overall weight of an
automobile. A composite material can be defined as an amalgamation of two or more materials that results in better properties than those of the individual components used alone. In contrast to metallic alloys, each material retains its separate chemical, physical, and mechanical properties. The two constituents are a reinforcement and a matrix. The main advantages of composite materials are their high strength and stiffness, combined with low density, when compared with bulk materials, allowing for a weight reduction in the finished part. The reinforcing phase provides the strength and stiffness. In most cases, the reinforcement is harder, stronger, and stiffer than the matrix [5]. M. Venkatesan et al., [6] in their work, have shown the design and experimental analysis of a composite leaf spring made of glass fiber reinforced polymer and compared to steel spring, 67.35% lesser stress and 76.4% weight reduction were found for the composite spring. K. K. Jadhao et al., [7] in their investigation considered glass fiber reinforced plastic (GFRP) and the polyester resin (NETPOL 1011) as the spring material and almost a reduction of 85% in weight was found after performing numerical and finite element analysis for the same. Mr. V. Lakshmi Narayana [8] proclaimed in her study regarding design and analysis of mono composite leaf spring for suspension in automobiles by using ProE & ANSYS that the composite leaf spring weighed only 27.96% of the steel leaf spring for the analyzed stresses. Sethilkumar Mouleswaran [9] performed design and experimental analysis of composite multi leaf spring using glass fibre reinforced polymer and the composite leaf spring is found to have 67.35% lesser stress, 64.95% higher stiffness and 126.98% higher natural frequency than that of existing steel leaf spring. The conventional multi leaf spring weighs about 13.5 kg whereas the E-glass/Epoxy multi leaf spring weighs only 4.3 kg. Thus the weight reduction of 68.15% is achieved. S. Venkatesh et al., [10] research work describes about the development of porous Aluminium foam for making commercial vehicle leaf spring made of Aluminium. The Aluminium foamed leaf spring has stresses much lower than steel leaf spring and weight of aluminium foamed leaf spring was reduced up to 20% using FEA stress and deflection analysis. M. M. Patunkar et al., [11] described that under the same static loading conditions, deflection and stresses of steel leaf spring and composite spring are found to have a great difference indicating reduction in weight by 84.40% under the same level of performance. M. Raghavedra et al., [12] performed design and analysis of laminated composite mono leaf spring. Compared to mono steel leaf spring the laminated composite mono leaf spring have 47% lesser stresses, 25%~65% higher stiffness, 27%~67% higher frequency and weight reduction of 73%~80%. Y. N. V. Santhosh Kumar et al., [13] in their work observed that the composite leaf spring weighed only 39.4% of the steel leaf spring for the analyzed stresses. Hence the weight reduction obtained by using composite leaf spring as compared to steel was 60.48%. Hence, surely composite materials may be able to provide a better performance and efficiency in the practical applications but, from manufacturing point of view we must admit that they are more expensive than that of steel. That’s why extending the research work performed by Rohit Ghosh et al., [1] the present exertion completely dismisses the proposition associated with manufacturing the complete spring by composites; but maintains its intense focus to manufacture those parts which are relatively more stressed as well as to maintain conventional materials for the lesser stressed parts to achieve an optimum extent towards the manufacturing costs. In the present work, the full-length leaves of a multi-leaf spring, which exhibit more stresses, were modelled separately with composites apart from the graduated length leaves where conventional steel is maintained and the entire system is combinedly analysed by using proper contact constraints under similar conditions in ANSYS software.

II. MATHEMATICAL FORMULATIONS

For the purpose of analysis, the leaves are divided in two groups as master leaf along with graduated length leaves forming one group and the extra full-length leaves forming the other group.

Let,

\[
\begin{align*}
n_f &= \text{number of extra full-length leaves}, \\
n_g &= \text{number of graduated-length leaves including the master leaf}, \\
n &= n_f + n_g = \text{Total number of leaves present in the multi-leaf spring}, \\
b &= \text{width of each leaf (mm)}, \\
t &= \text{thickness of each leaf (mm)}, \\
L &= \text{half the length of the semi-elliptic spring or the length of the cantilever (mm)}, \\
P &= \text{force applied at the end of the spring (N)}, \\
P_f &= \text{portion of } P \text{ taken by the extra full-length leaves (N)}, \\
P_g &= \text{portion of } P \text{ taken by the graduated-length leaves (N)}, \\
S_0P &= P_f + P_g
\end{align*}
\]

Now, from practical considerations for an automobile leaf spring, that is of semi-elliptical shape usually, for a length of 2L and a load of 2P acting at the centre, the entire beam can be considered as a double cantilever. If the leaves are cut into two equal halves in longitudinal plane and then combined accordingly, to form almost a triangular plate then, the maximum bending stress is given by [14-15].

\[
\text{Stress} = \frac{6P}{bLt}
\]
The bending stress in the graduated-length leaves is given by [3]

\[(S_b)_g = \frac{6P.L}{\pi b t^2} \] .........................................................................................(1)

The bending stress in the extra full-length leaves is given by [3]

\[(S_b)_f = \frac{18P.L}{3\pi n_f + 2n_g} \] .........................................................................................(2)

The maximum deflection of the spring is given by [3]

\[\delta = \frac{12P.L^3}{E(3n_f + 2n_g)bt^3} \] .........................................................................................(4)

It is to be noted that, the maximum bending stress occurs at the supports for such a plate. The aboverelations hold good for the leaves (or plates), having uniform cross-section. Also, it is seen that the bendingstresses in extra full-length leaves are 50% more than that of the graduated length leaves i.e. \((S_b)_f = 1.5(S_b)_g \) [3].

Calculation of length of different leaves:
For the calculation of length of different leaves, following relations were used and subsequently, the resultswere implemented while modeling the multi-leaf spring in CATIA V5R18 software.

Length of the smallest leaf = 1 * \[
\frac{\text{Effective length}}{n-1} + \text{Ineffective length}
\]

Length of the next leaf = 2 * \[
\frac{\text{Effective length}}{n-1} + \text{Ineffective length}
\]

Similarly, Length of the \((n-1)\)th leaf = \(n-1\) * \[
\frac{\text{Effective length}}{n-1} + \text{Ineffective length}
\]

Length of master leaf = \(2L + 2P(d + t)\)

Ineffective length = Distance between the centres of U-bolts = 1, Effective length = \(2L - 2\frac{1}{3}t\) and \(d\) = inside diameter of eye [2].

Apart from the above formulations, when a unidirectional continuous-fiber lamina or laminate is loaded in a direction parallel to its fibers (0° or 11-direction), the longitudinal modulus \(E_{11}\) can be estimated from its constituent properties by using the rule of mixtures [5]:

\[E_{11} = E_f V_f + E_m V_m,\]

where, \(E_f\) is the fiber modulus, \(V_f\) is the fiber volume percentage, \(E_m\) is the matrix modulus, and \(V_m\) is the matrix volume percentage.

The longitudinal tensile strength \(s_{11}\) also can be estimated by the rule of mixtures [5]:

\[s_{11} = s_f V_f + s_m V_m,\]

Where \(s_f\) and \(s_m\) are the ultimate fiber and matrix strengths, respectively. Because the properties of the fiber dominate for all practical volume percentages, the values of the matrix can often be ignored. So, the rule of mixtures has formed the basis for composite analysis during the simulation of the extra full-length leaves, which were again combinedly examined in the software with the graduated leaves made of steel as a single unit.

**III. DESIGN SPECIFICATION**

The objective of the present course of study includes, determination of maximum bending stress for threedifferent loading conditions for both the cases of steels and composites and to establish the relationship for the magnitude of bending stresses existinig the graduated-length leaves and extra full-length leaves (i.e. \((S_b)_f = 1.5(S_b)_g \) ), with the following dimensional specifications.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Value</th>
<th>Notation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Total length of the semi-elliptic spring (distance between two eyes)</td>
<td>1243 mm</td>
<td>2L</td>
</tr>
<tr>
<td>width of each leaf</td>
<td>100 mm</td>
<td>B</td>
</tr>
<tr>
<td>thickness of each leaf</td>
<td>14 mm</td>
<td>T</td>
</tr>
<tr>
<td>number of extra full-length leaves</td>
<td>2</td>
<td>(n_f)</td>
</tr>
<tr>
<td>number of graduated-length leaves including the master leaf</td>
<td>8</td>
<td>(n_g)</td>
</tr>
<tr>
<td>Total number of leaves present in the multi-leaf spring</td>
<td>10</td>
<td>N</td>
</tr>
<tr>
<td>Load acting at the centre of the spring</td>
<td>15000 N, 10000 N, 5000 N</td>
<td>2P</td>
</tr>
</tbody>
</table>
The dimensions are taken from practical understanding and the standards available in the market. For the first case, Structural steel was considered as the entire leaf material with an elastic modulus $E = 2.1 \times 10^5$ MPa, tensile yield strength $S_{yt} = 250$ MPa and Poisson’s ratio $= 0.3$ while performing the analysis in ANSYS(Workbench 16.2) software. In the next case, Carbon fiber steel has been considered as the material for the full-length leaves (fiber lamina or laminate is loaded in a direction parallel to its fibers) whereas, material for the rest of the leaves were kept same i.e. structural steel. For Carbon fiber steel, an Elastic Modulus $E = 2.64 \times 10^5$ MPa and ultimate strength $S_{ut} = 540$ MPa (at dry room temperature) were considered for simulation purpose; determined on the basis on rule of mixtures.

### IV. ANALYTICAL CALCULATION

From the relation of maximum bending stress $(s_b)_{\text{max}}$ and based on the above design specifications, the analytical calculation is carried out for the load of 15000 N. From equation (1) the maximum bending stress is given by,

$$(s_b)_{\text{max}} = \frac{6PL}{nht^2}$$

We have, $2P = 15000$ N, $2L = 1243$ mm, $n = 10$, $b = 100$, $t = 14$ mm, then

$$(s_b)_{\text{max}} = \frac{6 \times (15000/2) \times (1243/2)}{10 \times 100 \times 14^2} = 142.691 \text{ MPa}$$

Subsequently, the maximum bending stresses were evaluated for the loads of 10000 N, 5000 N and presented in Table: II. For the composite analysis part, as we know, when a unidirectional continuous-fiber lamina or laminate is loaded in a direction parallel to its fibers (0° or 11-direction), the longitudinal modulus $E_{11}$ can be estimated from its constituent properties by using what is known as the rule of mixtures [5]:

$$E_{11} = E_f V_f + E_m V_m,$$

where $E_f$ is the fiber modulus, $V_f$ is the fiber volume percentage, $E_m$ is the matrix modulus, and $V_m$ is the matrix volume percentage. The longitudinal tensile strength $s_{11}$ also can be estimated by the rule of mixtures:

$$s_{11} = s_f V_f + s_m V_m,$$

where $s_f$ and $s_m$ are the ultimate fiber and matrix strengths, respectively. Considering, $V_f = 0.6$, $V_m = 0.4$, $E_f = 3.0 \times 10^5$ MPa, $E_m = 2.1 \times 10^5$ MPa, $s_f = 600$ MPa, $s_m = 450$ MPa [20-21] we get,

$$E_{11} = 0.6 \times 3.0 \times 10^5 + 0.4 \times 2.1 \times 10^5 = 2.64 \times 10^5 \text{ MPa}$$

$$s_{11} = 0.6 \times 600 + 0.4 \times 450 = 540 \text{ MPa}$$

### V. MODELLING and SIMULATION

The objective of this analysis is to investigate the stresses in the laminated spring within the desirable limits to obtain a practical understanding for the theoretical ideas associated with composite materials. After geometric modeling in CATIAV5R18 software the spring is subjected to static analysis, performed in ANSYS (Workbench 16.2) software.

#### A. Modelling

The computer compatible mathematical description of the geometry of the object is called geometric modeling. CATIA is basically CAD (computer-aided design) software that allows the mathematical description of the object to be displayed and manipulated as the image on the monitor of the computer [16-17]. While modeling the spring, the full length leaves were designed separately as a different part body shown in Fig. 1, 2, 3; which were again combined with rest of the leaves in Ansys software through proper contact constraints.
ANSYS is an engineering simulation software that predicts with confidence about the performance of the product under the real-world environments incorporating all the existing physical phenomena [18-19]. While performing the part of composite analysis, the composite properties were imposed only in these full-length leaves by incorporating the new value of elastic modulus obtained from the rule of mixtures. The layout of static analysis involves meshing, boundary conditions and loading.

**B. Meshing**

Meshing is basically the division of the entire model into small elements. In order to maintain the shape, it is convenient to select the free mesh, as the geometry of leaf spring contains sharp curves. Element size of 20 mm with medium smoothing was considered for mesh generation. Minimum edge length of the elements was 14 mm. Within the solution domain under the Adaptive Mesh Refinement segment, Max. Refinement Loops was taken as 3 and Refinement Depth as 2. For the convergence plot, the maximum allowable change was considered as 4%. All the 44 faces were selected for mesh generation and total number of nodes and elements were observed as 13423 and 7358 respectively. Fig. 4 shows the meshed model of laminated spring.
C. Boundary Conditions
The leaf spring is mounted on the axle of an automobile. The frame of the vehicle is connected to the ends of the leaf spring. The ends are constructed in such a way that they form an eye-like structure. The front eye of the spring is directly connected with the frame by means of a simple pin joint; hence, it can freely rotate about the pin but is restricted for any kind of translation and rotation in all the other directions. Sounder the static structural domain of ANSYS software, the Remote Displacement was inserted and except rotation about X-axis, all other motions were constrained to set the above boundary condition. Now, the rear eye of the leaf spring is connected with the frame through a flexible link known as shackle. So, it has the flexibility to slide along the length of the spring and also to rotate about the pin. These were again established through Remote Displacement by setting Y-direction as unconstrained for translation according to the geometry, while keeping all other translatory motions restricted and rotation about X-axis was set free as before, keeping all other rotational motions constrained for the rear eye of the spring.

D. Load
The load is uniformly distributed by all the nodes associated with the bottom surface of the bottommost leaf. The Load is applied along FZ direction as shown in Fig. 5. To apply the load, under the static structural domain of ANSYS Software, Force was introduced and the magnitude of load was given for Z-direction. Here, we have considered a load of 5000 N is acting on the bottommost leaf.

![Fig. 4. Meshed model of the laminated spring](image)

![Fig. 5. Loading (5000 N) of the laminated spring](image)
VI. RESULTS and DISCUSSIONS

After performing the static analysis for both the cases of structural Steel and Carbon Fiber Steel for given dimensional specifications, the results obtained are summarised as follows:

A. Weight reduction:
Apart from the other benefits, the biggest benefit, however, is mass reduction for using composite materials for the full-length leaves. While, the mass for the laminated spring assembly was 89.447 kg before applying composites; for the next case on application of the same for full-length leaves, reduced the mass to 79.99 kg. So, almost a reduction of 10 kg can be obtained with the new construction method which can provide a great help towards the modern automobile industry that is increasingly focussing on weight reduction.

B. Maximum equivalent (von-Mises) stress:
Simulations were carried out for the three different loading conditions and the results obtained were similar in nature indicating a comprehensible trend towards the decreasing value of maximum equivalent (von-Mises) stress for composite applications. The experimental results obtained are conveyed as follows:

![Image of equivalent stresses distribution for structural steel](image1.png)

**Fig. 6.** Distribution of equivalent (von-Mises) stresses at a load of 5000 N for structural steel

![Image of equivalent stresses distribution for composite applications](image2.png)

**Fig. 7.** Distribution of equivalent (von-Mises) stresses at a load of 5000 N for composite applications
Fig. 8. Distribution of equivalent (von-Mises) stresses at a load of 10000 N for structural steel

Fig. 9. Distribution of equivalent (von-Mises) stresses at a load of 10000 N for composite applications

Fig. 10. Distribution of equivalent (von-Mises) stresses at a load of 15000 N for structural steel
A graph is plotted for the conventional steel and Composite based results with load on X-axis and stress values on Y-axis, shown in the following Fig. 12. There is a clear tendency towards stress reduction for the application of carbon fiber in the full length leaves.

The software based analysis was performed for the three different loading conditions and the results obtained were similar in nature indicating a comprehensible trend towards the decreasing value of Directional deformation for composite applications. The experimental results obtained are conveyed as follows:
Fig. 14. Distribution of directional deformation at a load of 5000 N for composite applications

Fig. 15. Distribution of directional deformation at a load of 10000 N for structural steel

Fig. 16. Distribution of directional deformation at a load of 10000 N for composite applications

Fig. 17. Distribution of directional deformation at a load of 15000 N for structural steel
A graph is plotted for the conventional steels and Composite based results with load on X-axis and directional deformation values on Y-axis, shown in the following Fig. 19. There is a clear tendency towards the reduction of directional deformation for the application of carbon fiber in the full length leaves.

D. Bending Stress distribution across the leaves:

In order to demonstrate the variation of bending stresses in different leaves at a particular load, we will take the help of the following Fig. 20. Using the Probe feature of ANSYS software, the stresses 7.578, 0.55374 and 3.9708 (in MPa) in three different locations at a particular cross-section are shown in the Fig. 20. For a load of 15000 N for structural steels. It can be clearly observed that, the stress value of 7.578, (MPa) associated with the extra full-length leaves are almost more than 1.5 times than that of the stress value of 3.9708 (MPa) corresponding to the graduated length leaves; and both the locations are almost equidistant from the minimum stress value point (0.55374) as shown. So, the nature of the result confirms the fact that, in contrast to uniform linear distribution of stress for simply supported beams from the neutral plane here, a nonlinear tendency is been observed due to the presence of full-length leaves exhibiting relatively higher stresses even being at a equal distance from the minimum stress value point. For more accurate positioning the result may approach towards the exact theoretical results; as we know of the stress being 1.5 times in full-length leaves than that of the graduated.
Again with the help of Probe tool, the stress values approximately at a particular cross-section have been shown above in Fig. 21, for composite application at a load of 15000 N. The value associated with the extra-full length leaves is 6.5889 (in MPa) and that for graduated leaves is 4.5878 (in MPa) from an equidistant minimum stress value point of 0.56291 (in MPa). So it has been observed that for composite applications, the stresses at full-length leaves have been reduced significantly from its previous value 7.578 (in MPa) associated with conventional steels which confirms our proposal as well as different research works performed earlier. The software based results are summarised as follows:
Table II : Comparison for steel and composite applications

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Load (in newton)</th>
<th>Steel application for the entire spring</th>
<th>Composite application for full-length leaves maintaining Steel for rest of the part</th>
<th>% change reduction</th>
</tr>
</thead>
<tbody>
<tr>
<td>Max. Equivalent (von-Mises) stress (in MPa)</td>
<td>15000</td>
<td>142.83</td>
<td>138.90</td>
<td>2.751523</td>
</tr>
<tr>
<td></td>
<td>10000</td>
<td>95.223</td>
<td>92.602</td>
<td>2.752486</td>
</tr>
<tr>
<td></td>
<td>5000</td>
<td>47.611</td>
<td>46.301</td>
<td>2.751465</td>
</tr>
<tr>
<td>Directional deformation (in mm)</td>
<td>15000</td>
<td>0.262</td>
<td>0.25277</td>
<td>3.522901</td>
</tr>
<tr>
<td></td>
<td>10000</td>
<td>0.52412</td>
<td>0.5055</td>
<td>3.552622</td>
</tr>
<tr>
<td></td>
<td>5000</td>
<td>0.78618</td>
<td>0.75832</td>
<td>3.543718</td>
</tr>
<tr>
<td>Mass (in kg)</td>
<td>-</td>
<td>89.447</td>
<td>79.99</td>
<td>10.572</td>
</tr>
</tbody>
</table>

VII. CONCLUSION and FUTURE SCOPE of WORK

In the present work, the laminated spring is modeled in CATIA V5R18 and same were analyzed in the Static structural domain of ANSYS software. The results were discussed in the preceding section and it is concluded that, for the given design specifications the values of maximum stresses at different loading conditions are well within the safe limits. Apart from that, most crucially the new construction method has proposed to manufacture the full-length leaves separately with composites in contrast to use of composites for the entire spring. From the software based results, we observed a comprehensible decreasing trend toward the stress and deformation values for composite applications. A mass reduction of more than 10% being the biggest benefit with the new method; we also achieve an optimum extent towards the manufacturing costs as composites being highly expensive [22-23] than that of steels (almost 2-3 times costlier). So, the new method seems to be beneficial exclusively for modern auto industry as it provides an optimum solution towards weight reduction as well as manufacturing costs; finally leading towards a level of greater customer satisfaction.

An extended study can be carried out on the topic in the context of different joining methods for metals with composites if we implement the proposed construction methodology for the spring. Mechanical Fasteners, adhesives or both can be used to join composites [24], but to choose the most effective onerequires an extensive effort for the same. Apart from that, the various factors associated with working conditions need to be considered as well.

REFERENCES


[23] [Online], Available: www.google.co.in/webhp?sourceid=chrome-instant&ion=1&espv=2&ie=UTF-8&q=cost%20of%20steel%20per%20square%20foot