Testing Effort Dependent Delayed S-shaped Software Reliability Growth Model with Imperfect Debugging

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Abstract—In software development process, testing is one of the most important aspects and hence, software reliability is very important factor of software systems. In the last four decades many software reliability growth model based on non-homogeneous Poisson process (NHPP) have been developed which incorporates testing effort function. However, the previous models are quite helpful for software engineers/developers and commonly applicable in the industries and research institution. Still more testing-effort functions are required to incorporate into software reliability growth model. In this paper, we develop delayed S-shaped software reliability growth model with imperfect debugging which incorporates new modified Weibull testing–effort function (NMWTEF). We estimate the testing effort model parameters by least square and S-shaped software reliability growth parameters by maximum likelihood estimation techniques. We also present confidence interval of the software reliability growth parameters. Various software reliability measures are investigated through three numerical experiments. The numerical results are compared with other existing models in the literature. It is shown that the proposed Delayed S-shaped Software Reliability Growth Model with imperfect debugging with NMWTEF has a fairly better errors prediction capability.

Keywords—Software Testing, Software Reliability Growth, Testing Effort Functions, Least Square estimation, Maximum Likelihood estimation

I. INTRODUCTION

Software reliability is one of the important factors of software quality. Before software delivered in to market it is thoroughly checked and errors are removed. Every software industry wants to develop software that should be error free. Software reliability growth models use measured trends of failure rates (or change in intervals between failures) and extrapolate them to future operation. In most cases, they evaluate the reduction in failure frequency during successive developmental test intervals to estimate the software reliability at the conclusion of the test (and sometimes into operational deployment).

Software reliability is defined according to as the probability of failure free operation of a computer program in a specified environment for a specified period of time. A software reliability growth model (SRGM) explains the time dependent behavior of fault removal. The objective of software reliability testing is to determine probable problems with the software design and implementation as early as possible to assure that the system meets its reliability requirements. Numerous SRGMs have been developed during the last three decades and they can provide very useful information about how to improve reliability (Musa et al., 1987; Xie, 1991; Lyu, 1996). Among these models, exponential growth model, inflection S-shaped and delayed S-shaped growth model have been shown to be very useful in fitting software failure data. Many authors has incorporated testing-effort into exponential type and inflection S-shaped SRGM based on the NHPP to get a better description of the fault detection phenomenon (Pham, 2007; Pham et al. 1999; Yamada et al., 1984; 1986; 1987; 1993; Kapur and Garg, 1996; Kapur and Younes, 1994; Huang et al., 1997; 2007; Kuo et al., 2001; Huang and Kuo, 2002; Huang, 2005; Bokhari and Ahmad, 2006; 2007; 2014; Quadri and Ahmad, 2010; Quadri et al., 2006; 2008; Ahmad et al., 2008; 2009; 2010; 2010a 2011). Some authors have incorporated testing-effort into delayed S-shaped SRGM.
This paper incorporates New Modified Weibull Testing–effort function (NMWTEF) into delayed S-shaped NHPP growth models (Ohba, 1984; 1984a). The parameters of the model are obtained by Least Square Estimation (LSE) and Maximum Likelihood Estimation (MLE) methods. We present the analysis of real data in this paper and the results are compared with other models from literature.

II. SOFTWARE RELIABILITY GROWTH MODEL WITH NMWTEF

SRGM help to measure and track the growth of reliability as software is being improved. There is an extensive body of literature on software reliability growth modeling, with many detailed probability models purporting to represent the probabilistic failure process. The objective of software reliability testing is to determine probable problems with the software design and implementations. Often SRGM may also yield information on physical properties of the code, such as the number of faults remaining in a software system, etc. In general, the exposure time over which reliability is being assessed may be expressed as calendar time, clock time, CPU execution time, number of test-runs, or some other suitable measures. Exponential Growth Model and delayed S-shaped growth model have been shown to be very useful in fitting real software data.

A. NMW Testing Effort Function

The testing-effort indicates how the errors are detected effectively in the software and can be modeled by different distributions (Musa et al., 1987; Yamada et al., 1986; 1993; Kapur et al., 1999). Testing Effort Function describes the relationship between the effort expended to test software (e.g., in person-months), and the physical characteristics of the software, such as LOC, exposure time (which can take many forms, and can be expressed either as total effort), etc. The Cumulative NMWTEF expenditure consumed in (0, t) is depicted in the following (Quadri and Ahmad, 2010):

\[ W(t) = \alpha \cdot (1 - e^{-\beta t^m e^{\delta m} t}) , \alpha > 0, \beta > 0, m \geq 0, \delta > 0. \]  

Therefore, the current NMWTEF expenditure attesting t is given by:

\[ w(t) = \frac{dW(t)}{dt} = \alpha \cdot \beta \cdot (m + \delta \cdot t) \cdot t^{m-1} \cdot e^{\delta t} \cdot e^{-\beta t^m e^{\delta t}}. \]  

Where \( \alpha, \beta, m, \delta \) are constant parameters, \( \alpha \) is the total amount of testing-effort expenditures; \( \beta \) and \( \delta \) are the scale parameters, and m is shape parameter of NMW.

B. Delayed S-Shaped SRGM with NMWTEF

The Delayed S-shaped SRGM was originally proposed by Yamada et al. (1984). It was a simple modification of the NHPP to obtain an S-shaped growth curve for the cumulative number of failures detected. Software fault detection process can be viewed as a learning process that the software testers become familiar with the testing environments and tools as time progresses, these testers’ skills gradually improve and then level off as the residual faults become more difficult to uncover. Because the original S-shaped model is for the analysis of fault isolation data, i.e. the testing process contains not only a fault detection process, but also a fault isolation process. Recently, Huang et al. (2007) modified delayed S-shaped SRGM and testing effort function has also been incorporated in the SRGM.

The extended delayed S-shaped model with NMWTEF is formulated on the following assumptions,

1. The fault removal process follows the NHPP.
2. The software system is subject to failures at random times caused by faults remaining in the systems.
3. The mean number of faults detected in the time interval \((t, t + \Delta t)\), by the current testing effort is proportional to the mean number of remaining faults in the software.
4. The proportionality of fault detection is constant.
5. The mean number of faults isolated in the time interval \((t, t + \Delta t)\) by the current testing effort is proportional to the current number of faults isolated in the software.
6. The proportionality of fault isolation is constant.
7. The consumption of testing-effort is modeled by NMWTEF.
8. Each time a failure occurs, the fault which caused it is immediately removed, and no new faults are introduced.

According to these assumptions, the extended Delayed S-Shaped SRGM can be formulated as:

\[ \frac{dm(t)}{dt} \times \frac{1}{w(t)} = r_1 \times [a - m_a(t)] \]  

and
\[
\frac{dm_r(t)}{dt} \times \frac{1}{w(t)} = r_2 \times [m_d(t) - m_r(t)]
\]  
(4)

If \( r_2 \neq r_1 \), then the solution of equations (3) and (4) under the boundary condition \( m_d(0) = 0 \) and \( m_r(0) = 0 \), are

\[
m_d(t) = a \times (1 - \exp[-r_2 W(t)])
\]

(5)

and

\[
m_r(t) = a \times \left\{ - \frac{r_1 \exp[-r_1 W(t)] - r_2 \exp[-r_2 W(t)]}{r_1 - r_2} \right\}
\]

(6)

Let \( r_2 \equiv r_1 \), then, the delayed S-shaped SRGM with TEF is given by

\[
m(t) = a \times (1 + r W(t)) \exp[-r W(t)]
\]

(7)

In other way, if we suppose

\[
r(t) = \frac{r^2 t}{1 + rt}
\]

(8)

Now substituting in to

\[
\frac{dm(t)}{dt} \times \frac{1}{w(t)} = r(t) \times [a - m(t)](a > 0)
\]

(9)

We get the following SRGM,

\[
\frac{dm(t)}{dt} \times \frac{1}{w(t)} = \frac{r^2 t}{1 + rt} \times [a - m(t)]
\]

(10)

Solving under the boundary condition \( m(0) = 0 \), obtain the same MVF as

\[
m(t) = a \times (1 + r W(t)) \exp[-r W(t)]
\]

(11)

III. ESTIMATION OF MODEL PARAMETERS

The success of a software reliability growth model depends heavily on the quality of the failure data collected. The parameters of the Software Reliability Growth Model are estimated based upon these data. In order to validate the proposed model and to compare its performances with other existing models, experiments on actual software failure data will be performed. MLE and LSE techniques are used to estimate the model parameters (Musa et al., 1987; Musa, 1999; Lyu, 1996). Sometimes, however, the likelihood equations may be complicated and difficult to solve explicitly. In that case one may have to solve with some numerical methods to obtain the estimates. On the other hand, Least Square Estimation (LSE), like Maximum Likelihood Method (MLE), is fairly general technique which can be applied in most practical situations for small or medium sample sizes and may provide better estimates (Musa et al., 1987; Huang et al., 1997; Huang and Kuo, 2002). It minimizes the sum of squares of the deviations between what we expect and what we actually observe.

A. Least Square Estimation Method

The parameters \( \alpha, \beta, m, \) and \( \delta \) in NMWTWF can be estimated by LSE method. These parameters are determined for \( n \) observed data pairs in the form \((t_k, W_k) (k = 1, 2, \ldots, n; 0 < t_1 < t_2 < \ldots < t_n) \), where \( \hat{\alpha}, \hat{\beta}, \hat{m}, \) and \( \hat{\delta} \) can be obtained by minimizing (Bokhari and Ahmad, 2006; Ahmad et al. 2008; 2009; 2010; 2011) the following equations:

\[
S(\alpha, \beta, m, \delta) = \sum_{k=1}^{n} [W_k - W(t_k)]^2
\]

(12)

B. Maximum Likelihood Method

Once the estimates of \( \alpha, \beta, m, \) and \( \delta \) are known, the parameters of the SRGMs can be estimated through Maximum Likelihood Estimation Method. The estimators of \( a \) and \( r \) are determined for the \( n \) observed data pairs in the form \((t_k, y_k) (k = 1, 2, \ldots, n; 0 < t_1 < t_2 < \ldots < t_n) \) where \( y_k \) is the cumulative number of software faults detected up to time \( t_k \) or \((0, y_k) \). Then the likelihood function for the unknown parameters \( a \) and \( r \) in the SRGM model (7) is given by (Musa et al. 1987).
\[ L = \prod_{i=1}^{n} \frac{[m(t_i) - m(t_{i-1})]^{(m_{i} - m_{i-1})}}{(m_{i} - m_{i-1})!} e^{-m(t_{i}) - m(t_{i-1})} \] (13)

where, \( m_0 \equiv 0 \) and \( t_0 \equiv 0 \).

MLEquations can be solved by numerical method to obtain the values of \( a \) and \( r \).

C Confidence Interval Estimation

Now the two sided confidence interval is as follows:

The \((1 - \alpha)100\%\) confidence limits for \( a \) and \( r \) is obtained as \(\text{(Yamada and Osaki, 1985)}:\)

\[
\hat{a} - z_{\alpha/2} \sqrt{\text{Var}(\hat{a})} \leq a \leq \hat{a} + z_{\alpha/2} \sqrt{\text{Var}(\hat{a})}
\] (14)

and

\[
\hat{r} - z_{\alpha/2} \sqrt{\text{Var}(\hat{r})} \leq r \leq \hat{r} + z_{\alpha/2} \sqrt{\text{Var}(\hat{r})}
\] (15)

where \( z_{\alpha/2} \) is the \((1 - \alpha/2)\)quartile of the standard normal distribution.

IV. COMPARISON CRITERIA

We can use the following three criteria to check the performance of proposed Software Reliability Growth Model with NMWTEF.

A. The Accuracy of Estimation (AE):

The Accuracy of Estimation is defined \(\text{(Musa et al., 1987; Kuo et al., 2001)}\) as

\[ AE = \left| \frac{M_a - \hat{a}}{M_a} \right| \] (16)

Where \( M_a \) is the actual cumulative number of detected error after the test, and \( a \) is the estimated number of initial errors. For practical purpose, a \( M \) is obtained from software error tracking after software testing.

B. The Mean of Squared Errors (MSE):

The Mean Square Errors defined as

\[ \text{MSE} = \frac{1}{k} \sum_{k=1}^{k} (m(t_i) - m_i)^2 \] (17)

where \( m(t_i) \) is the expected number of errors at time \( t_i \) estimated by a model, and \( m_i \) is the expected number of errors at time \( t_i \). MSE gives a quantitative comparison for long-term predictions. A smaller MSE indicates a minimum fitting error and better performance.

C. The Relative Error(RE):

The Relative Error can be calculated by given formula:

\[ \text{Relative Error} \ (RE) = \frac{m(t_e) - q}{q} \] (18)

Assume that we have observed \( q \) failures by the end of test time \( t_e \). We use the failure data up to time \( t_e \) to determine the parameters of \( m(t) \).

V. DATA ANALYSIS

In this section we are going to estimate the parameters of NMWTEF with real data sets. The models parameters are estimated by Least Square Estimation (LSE) and Maximum Likelihood Estimation (MLE) methods. The liner equation formed by LSE and MLE are solved numerically. Also, evaluate the different comparison criteria to check the performance of proposed software reliability growth models.

A. Data Set (DS1): This data is from the study of Ohba (1984). The system is PL/1 data base application software, consisting of approximately 1,317,000 lines of code. During the nineteen weeks experiments, 47.65 CPU hours were consumed and about 328 software errors were removed. The study reports that the total cumulative number of detected faults after a long period of testing is 358. In order to estimate the parameters \( a, \beta, \delta \) and \( m \) of the NMWTEF; we use the method of least squares. The following estimates are obtained
\[
\hat{a} = 64.4667, \hat{\beta} = 0.0341, \hat{\delta} = 0.885, \text{ and } \hat{m} = 0.056
\]  \tag{19}

Figure 1 shows the fitting of the estimated NMWTEF with the above estimates. The fitted curves and the actual software data are shown by solid and dotted lines, respectively.

Using the estimated parameters \(\alpha, \beta, m\) and \(\delta\), the parameters \(a, r\) in (7) can be obtained by the MLE method. The estimated values of the parameters \(a\) and \(r\) with confidence interval are given by:

\[
a = 352.719, r = 0.080
\]  \tag{20}

**Table I: Confidence Interval of Parameter Estimates for DS1**

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Estimate</th>
<th>95 percent Confidence Interval</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Lower bound</td>
</tr>
<tr>
<td>(a)</td>
<td>352.719</td>
<td>327.073</td>
</tr>
<tr>
<td>(r)</td>
<td>0.090</td>
<td>0.080</td>
</tr>
</tbody>
</table>

![Figure 1: Observed/estimated current testing-effort function vs. time.](image1)

Figure 2 illustrates a fitted curve of the estimated cumulative failure curve with the actual software data. The \(R^2\) value for NMWTEF is 0.99674. Therefore, it can be said that the proposed curve is suitable for modeling the software reliability.

**Table II** presents the comparisons of proposed model with different SRGMs which reveal that the proposed model has a good performance.

![Figure 2: Observed/estimated cumulative number of failures vs. time.](image2)
Table II: Comparison of different SRGMs for Data Set 1.

<table>
<thead>
<tr>
<th>Model</th>
<th>$a$</th>
<th>$r$</th>
<th>$AE%$</th>
<th>$MSE$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Proposed model</td>
<td>352.72</td>
<td>0.09</td>
<td>1.7</td>
<td>197.4</td>
</tr>
<tr>
<td>Yamada delayed S-shaped model</td>
<td>374.05</td>
<td>0.1976</td>
<td>4.48</td>
<td>168.67</td>
</tr>
<tr>
<td>Delayed S-Shaped with Logistic TEF</td>
<td>346.55</td>
<td>0.0936</td>
<td>3.20</td>
<td>147.61</td>
</tr>
<tr>
<td>Huang Logistic model</td>
<td>394.08</td>
<td>0.0427</td>
<td>10.69</td>
<td>118.59</td>
</tr>
<tr>
<td>G-O model</td>
<td>760.0</td>
<td>0.0323</td>
<td>112.29</td>
<td>139.82</td>
</tr>
</tbody>
</table>

Furthermore, the relative error in prediction of proposed model for the data set is calculated and illustrated by Figure 3. It is shown that relative error approaches zero as $t_e$ goes to. Therefore, Figure 2 to 3 and reveal that the proposed model has better performance than the other models.

![Figure 3: Predictive Relative Error Curve](image)

A. Data Set Second (DS2)

The second set of actual data in this research is the System T1 data of the Rome Air Development Center (RADC) projects and cited from Musa et al. (1987), Musa (1999). The number of object instructions for the system T1 which is used for a real-time command and control application. The size of the software is approximately 21,700 object instructions and developed by Bell Laboratories. The software was tested for twenty one weeks with 9 programmers. During the testing phase, about 25.3 CPU hours were consumed and 136 software errors were removed. The number of errors removed after 3.5 years of test was reported to be 188 (Huang, 2005). Similarly, parameters $\alpha, \beta, \delta$ and $m$ of NMWTEF for this data set can be obtained by using the method of LSE. The estimated values are

$$\hat{\alpha} = 25.587868, \hat{\beta} = 0.00009838, \hat{\delta} = 1.140123 \text{ and } \hat{m} = 0.33891$$

(21)

Using the estimated parameters $\alpha, \beta, \delta$ and $m$, the parameters $a, r$ in (7) can be obtained by the MLE method:

$$a = 124.824 \quad r = 0.4$$

(22)

Table III: Confidence interval of Parameter for DS2

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Estimate</th>
<th>95% Confidence Interval</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Lower Bound</td>
</tr>
<tr>
<td>$a$</td>
<td>124.824</td>
<td>112.530</td>
</tr>
<tr>
<td>$r$</td>
<td>0.400</td>
<td>0.296</td>
</tr>
</tbody>
</table>
Figure 4 shows the fitting of the NMWTEF whereas Figure 5 illustrates a fitted curve of the estimated cumulative number of failures. The fitted curve and the actual software data are shown by solid and dotted lines, respectively. The $R^2$ value for proposed NMWTEF is 0.9974. Therefore, it can be said that the proposed curve is suitable for modeling the software reliability.

Table IV gives the comparisons of proposed model with different SRGMs which reveal that the proposed model has better performance. Kolmogorov Smirnov goodness-of-fit test shows that the proposed SRGM fits pretty well at the 5 percent level of significance.

<table>
<thead>
<tr>
<th>Model</th>
<th>$a$</th>
<th>$r$</th>
<th>AE (%)</th>
<th>MSE</th>
</tr>
</thead>
<tbody>
<tr>
<td>Proposed model</td>
<td>124.8</td>
<td>0.40</td>
<td>33.62</td>
<td>155.3</td>
</tr>
<tr>
<td>Yamada delayed S-Shaped model</td>
<td>237.19</td>
<td>0.0963</td>
<td>26.16</td>
<td>245.24</td>
</tr>
<tr>
<td>Delayed S-Shaped model with Logistic TEF</td>
<td>124.11</td>
<td>0.411</td>
<td>33.98</td>
<td>180.02</td>
</tr>
<tr>
<td>G-O model</td>
<td>142.32</td>
<td>0.1246</td>
<td>24.29</td>
<td>2438.3</td>
</tr>
</tbody>
</table>

Lastly, the relative error in prediction of proposed model for this data set is calculated and shown graphically in Figure 6. The relative error is plotted against the percentage of data used (that is, $t_s / t_e$). Consequently, from the Figures 4 to 6 and Table IV, it can be concluded that the proposed model gets reasonable prediction in estimating the number of software faults and fits the observed data better than the others.
VI. IMPERFECT DEBUGGING

Software Testing is very much important in assuring the quality of the software by identifying and removing faults in software, to make the software more efficient. But testing of the software for a long time may not ensure a bug free software and high reliability. Optimum amount of code also needs to be covered to make sure that the software is of good quality. Testing time alone may not give the correct picture of the number of faults removed in the software. The faults in the software may not be removed perfectly; this is mainly due to complexity of software or nature of testing team. This phenomenon is known as imperfect debugging. When the faults are not removed perfectly and leads to further generation of faults, this process is known as error generation (Pham et al. 1999).

In this section, we discuss a relaxation of the perfect debugging assumption. We modify the assumption (8) of section 3:

\[
\frac{dm(t)}{dt} = \frac{1}{w(t)\Psi} r(t) \times \left[ n(t) - m(t) \right]
\]

(23)

or

\[
\frac{dn(t)}{dt} = \Psi \frac{dm(t)}{dt}
\]

(24)

when

\[
r(t) = \frac{r^2 t}{1 + rt}
\]

Solving equation (23) using equation (24) under the boundary condition \( m(0)=0 \), \( n(0)=a \), and \( W(0)\Psi=0 \), we obtain the delayed S-shaped MVF under imperfect debugging

\[
m(t) = \frac{a}{1 - \Psi \left[ 1 - (1 + rW(t))^{1 - \Psi} \exp \left( -r(1 - \Psi)W(t) \right) \right]}
\]

(25)

A. Illustrated Example: From the above imperfect debugging model, summary of estimated parameters with their 95% confidence interval for PL1(DS1) are presented in the Table V:

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Estimate</th>
<th>95% Confidence Interval</th>
</tr>
</thead>
<tbody>
<tr>
<td>a</td>
<td>7.746</td>
<td>-11.918 - 27.410</td>
</tr>
<tr>
<td>( \Psi )</td>
<td>0.984</td>
<td>0.940 - 1.028</td>
</tr>
<tr>
<td>r</td>
<td>1.688</td>
<td>-2.135 - 5.510</td>
</tr>
</tbody>
</table>

Table V. Parameter Estimates under Imperfect debugging
Table VI shows the estimated parameters of the proposed SRGM and some selected models for comparison under imperfect debugging. It also gives the value of MSE. We observed that the value of MSE of the proposed SRGM with NMW testing-effort function is the lowest among all the models considered. Moreover, the estimated values $\Psi$ of all the models is close to but not equal to zero, thus the error removal phenomenon may not be pure perfect debugging process. A fitted curve of the estimated cumulative number of failures with the actual software data and the RE curve for the proposed SRGM with NMWTEF under imperfect debugging is illustrated by Figure 7 and 8.

### Table VI. Comparison with different SRGMs under Imperfect Debugging

<table>
<thead>
<tr>
<th>Models</th>
<th>$a$</th>
<th>$r$</th>
<th>$\Psi$</th>
<th>MSE</th>
</tr>
</thead>
<tbody>
<tr>
<td>Proposed model</td>
<td>7.746</td>
<td>1.688</td>
<td>0.984</td>
<td>91.04</td>
</tr>
<tr>
<td>Huang Logistic model</td>
<td>391.62</td>
<td>$4.20 \times 10^{-2}$</td>
<td>$1.16 \times 10^{-2}$</td>
<td>114.09</td>
</tr>
<tr>
<td>Huang Rayleigh model</td>
<td>399.02</td>
<td>$3.16 \times 10^{-2}$</td>
<td>$1.23 \times 10^{-2}$</td>
<td>268.55</td>
</tr>
<tr>
<td>Delayed S-Shaped model with logistic TEF</td>
<td>335.39</td>
<td>$1.24 \times 10^{-1}$</td>
<td>$1.15 \times 10^{-2}$</td>
<td>634.60</td>
</tr>
<tr>
<td>Delayed S-Shaped model with Rayleigh TEF</td>
<td>346.09</td>
<td>$9.88 \times 10^{-2}$</td>
<td>$1.39 \times 10^{-2}$</td>
<td>880.49</td>
</tr>
<tr>
<td>Extended Goel-Okumoto model</td>
<td>365.85</td>
<td>$7.53 \times 10^{-2}$</td>
<td>$2.87 \times 10^{-1}$</td>
<td>222.09</td>
</tr>
</tbody>
</table>

![Figure 7: Observed/estimated cumulative number of failures v. time](image1)

![Figure 8: Predictive Relative Error Curve](image2)
VII. CONCLUSION

This paper proposed a SRGM based on NHPP model, which incorporates NMW testing-effort function into delayed S-shaped model. The performance of the proposed SRGM is compared with other existing SRGMs using different criteria. The results show that the proposed model has good performance, better fit and wider applicability based on two real data applications. We conclude that the incorporated NMWTEF into delayed S-shaped model is a flexible and can be used to describe the actual expenditure patterns more faithfully during software development.

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ISSN : 0975-3397
Vol. 9 No.05 May 2017
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