

A Hybrid Intelligent System for Fruit Grading and Sorting

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Abstract- Agriculture and food industry are the backbone of any country. Fruit industry is the prime contributor in agricultural sector. Thus, automation of fruit grading and sorting is the need of the hour. Since, artificial neural networks are best suited for automated pattern recognition problems; they are used as a classification tool for this research. Back propagation is the most important algorithm for training neural networks. But, it easily gets trapped in local minima leading to inaccurate solutions. Therefore, some global search and optimization techniques were required to hybridize with artificial neural networks. One such technique is Genetic algorithms that imitate the principle of natural evolution. So, in this article, a hybrid intelligent system is proposed for fruit grading and sorting in which artificial neural networks are merged with genetic algorithms. Results show that proposed hybrid model outperformed the existing back propagation based system.

Keywords: Fruit grading and sorting; artificial neural networks; Genetic algorithms; Hybrid intelligent system; Pattern recognition

I. INTRODUCTION

Fruit industry plays an important role in the economic development of a country. To this day, the practices followed to grade and sort fruit in India, are the traditional one. Manual inspection through an expert is still the common approach for fruit grading. However, these methods are quite time consuming and a good human effort is required. Hence, there is an immense need of an automated fruit grading system that apart from being accurate should be cost effective and fast.

In fruit grading/sorting systems, classification is the chief concern. Artificial neural networks are apt to provide optimal solutions to classification problems. Besides, their ability to learn from past data and to perform in non-linear domain makes them well suited for fruit grading applications. In general, artificial neural networks (ANN) are an attempt at simulating the human brain. The principle method to train multi-layer neural networks is the back propagation algorithm (BPA). It is a gradient descent method that sometimes, gets trapped in local solutions. This further leads to slow training and scaling issues [12]. Consequently, a global search and optimization approach was required to merge with back propagation algorithm. One such candidate is genetic algorithms.

Genetic algorithms (GA) are stochastic, population based search algorithms that imitate the principle of evolution. They are based on Darwinian Theory of evolution: 'survival of the fittest'. Moreover, they provide global optimum solution to complex problems without human intervention [4]. This is the foremost reason to hybridize them with artificial neural networks. Through this article, a hybrid (BP/GA) intelligent system is proposed so as to utilize the merits of ANN as well as GA for accurate fruit grading and sorting.

The remaining article is organized as follows: a brief literature survey is provided in Section 2, details of proposed model and methodology are given in Section 3, results and discussions are presented in Section 4, and the conclusions are summarized in Section 5.

II. LITERATURE REVIEW

Fruit grading and sorting was performed for variety of fruits such as apple, banana, watermelon, pomegranate, date, chili, grapes, blueberry, peach and many more. In the field of artificial neural networks, a number of contributions could be found. Bennedsen et al. (2007) detected surface defects for apple fruit in near infrared images utilizing artificial neural networks with principal component analysis. An accuracy rate of 79% was achieved. Likewise, Unay and Gosselin (2005) developed a neural networks based defect detection-cum-grading system for apple fruit. The system achieved 89.9 % accuracy in classifying the defects. Another effort was done by Cetişli and Büyükçingir (2013) who proposed a novel model to predict the early appearance of apple scab based on neuro-fuzzy classifier.

Ohali (2011) developed grading model using back propagation neural networks as classification tool. The main cultivar was date fruit. Similarly, Khalid and Tamer (2012) employed two variants of neural networks: back propagation algorithm and radial basis function to classify date fruit varieties. Janik et al. (2007) compared the performance of partial least squares (PLS) regression analysis and ANN for grapes in visible-near-infrared

spectra. Another attempt to compare the performance of ANN was by Motaveli et al. (2010). The authors compared different mathematical models with ANN for predicting the drying of pomegranate. It was established that ANN performed well as compared to respite mathematical models under study.

Yet another classification model was proposed by Llobet et al. (1999) to predict the ripeness of bananas using electronic nose sensors. Three different classifiers (Fuzzy ARTMAP, LVQ and ANN) were compared. While working for orange fruit, Rasekhi and Raoufat (2011) evaluated the performance of three ANN models: variable learning rate back propagation (MLP-GDM), resilient back propagation (MLP-RP) and scaled conjugate gradient (MLP-SCG). MLP-RP and MLP-SCG models outperformed the simple gradient back propagation algorithm. In a similar attempt, Mercol et al. (2007) performed orange fruit classification using five decision trees (J48, Classification and Regression Tree (CART), Best First Tree, Logistic Model Tree (LMT) and Random Forest), two neural network models (BPA, RBF) and Support Vector Machines.

Salim et al. developed a non-destructive mango fruit ripeness prediction model using gas sensors. ANN was effectively trained to classify mangoes according to different ripeness stages. One more contribution was by Zakaria et al. (2012) to evaluate the maturity of mangoes. Here Linear Discriminant Analysis (LDA) was hybridized with ANN to discriminate the mango harvested at week 7 and week 8.

A handful of contributions were made in the field of fruit grading using artificial neural networks. However, little emphasis was given to improve the classification accuracy of the models. Perhaps, this could be a possible reason for availability of very few contributions related to optimization of classifiers. So, the present research tries to achieve two objectives: one is to hybridize ANN with GA to eliminate the merits of BPA; and the other is to implement the hybrid model for accurate fruit grading and sorting model.

III. MATERIALS AND METHODS

The hybrid fruit grading model comprised of five major phases: Image acquisition, pre-processing, segmentation, feature extraction and classification, as shown in figure 1.

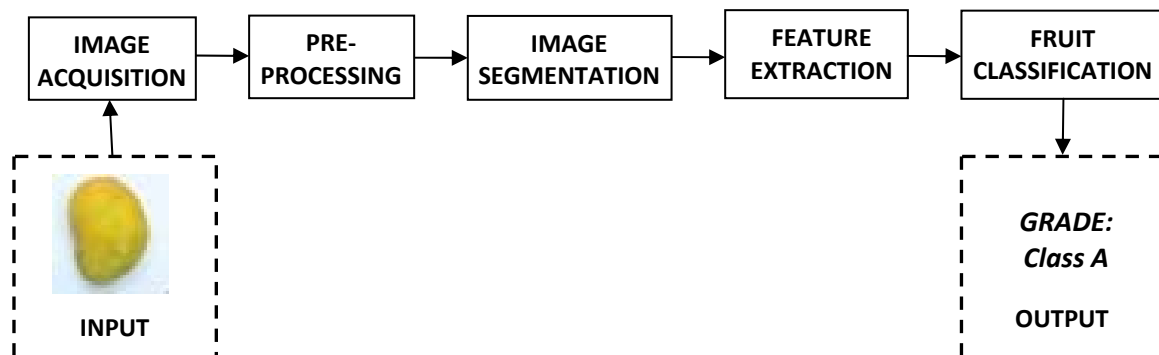


Figure 1: Block Diagram of Fruit Grading Model

A. Image Acquisition

The model initiated with the image acquisition task. Mango is chosen as a sample fruit for the model. Own camera set-up was used to acquire mango images. A Nikon camera (model: D7000) was used for acquiring the images. Afterwards, a database was prepared to store the mango images for further use.

B. Pre-processing

The next task after image acquisition was the resizing and cropping of images to a fixed size. All the images were resized to same dimensions of 100×100 . Then the images were enhanced using Wiener filter. The reason for using Wiener filter was that it adjusts itself according to the local intensity variance in the image. The filter performed less smoothing for regions of large intensity variance and more smoothing for regions of small variance values. Therefore, the filter was very well suited for fruit grading applications where fruit edges were to be retained while small bruises on the surface were to be smoothed off.

C. Segmentation

In the proposed model, segmentation was the third and most important task. Otsu threshold-based method [11] was used for separating the fruit object from the rest of the image. The steps of the algorithm are given in figure 2.

1. Compute histogram and probabilities of each intensity level.
2. Set up initial class probability $\omega_i(0)$ and class mean $\mu_i(0)$.
3. Step through all possible thresholds $t=1\dots$ maximum intensity:
 - 3.1. Update ω_i and μ_i .
 - 3.2. Compute intra-class variance $\sigma_b^2(t)$
4. Desired threshold corresponds to the maximum $\sigma_b^2(t)$.
5. Compute two maxima (and two corresponding thresholds). $\sigma_{b1}^2(t)$ is the greater max and $\sigma_{b2}^2(t)$ is the greater or equal to maximum.
6. Compute Desired threshold = $\frac{\text{threshold}_1 + \text{threshold}_2}{2}$.

Figure 2: Steps of Otsu Segmentation

D. Feature Extraction

As discussed earlier, Otsu segmentation was performed to obtain the object of interest from the image. Thereafter, feature extraction was performed, in which, two different set of features were extracted, namely, color based and shape based. Six color based features were obtained: mean of R, G and B components and standard deviation of R, G and B components of colored image. Six shape based features were extracted: Area, major axis, minor axis, eccentricity, perimeter-O, and perimeter-S. Two perimeter values were taken. Perimeter-O denotes perimeter value of object of interest obtained after Otsu segmentation and Perimeter-S denotes perimeter value of fruit as well as defect (if any) on the fruit surface. To compute perimeter-S, some edge detection technique was to be employed. In the proposed system, Sobel edge detection[15]operator was used. The basic idea behind perimeter compute was to grade the fruit according to its color, shape and defect. Color and shape were directly obtained from features, but, defect was indirectly obtained by comparing the Otsu perimeter and Sobel perimeter. If there is difference in perimeter values, the defect is present else the fruit is non-defective. The details of features are provided in table 1.

Table 1: Details of Features Extracted for Fruit Grading Applications

Type	Feature	Description	Formula
1. Color based features	Mean_R	Mean of 'R' component	$\mu = \frac{\sum_i^M \sum_j^N x}{M.N}$
	Mean_G	Mean of 'G' component	
	Mean_B	Mean of 'B' component	
	Std_R	Standard deviation of 'R' component	$SD = \sqrt{\frac{1}{n-1} \sum_i^n (x_i - \bar{X})^2}$
	Std_G	Standard deviation of 'G' component	
	Std_B	Standard deviation of 'B' component	
2. Shape based features	Area	Number of pixels in the region described by the shape	$Area = \sum_{x,y} I(x,y)$
	Major axis	Largest distance connecting one point to another on the region boundary, going through the center of the region.	---
	Minor axis	Smallest distance connecting one point to another on the region boundary, going through the center of the region.	---
	Eccentricity	Measure of aspect ratio	$Ecc = \frac{\text{major axis}}{\text{minor axis}}$
	Perimeter-O	Distance around the boundary of object, calculated from Otsu segmented image. It consisted fruit boundary only.	$Perimeter = \sum_{x,y} x_i - x_{i+1} $
	Perimeter-S	Distance around the boundary of object, calculated from Sobel segmented image. It included defect as well as fruit boundary	$Perimeter = \sum_{x,y} x_i - x_{i+1} $

E. Classification

Classification was the final step. It was performed using the hybrid genetic algorithm based back propagation approach. The block diagram of the classification algorithm is shown in figure 3.

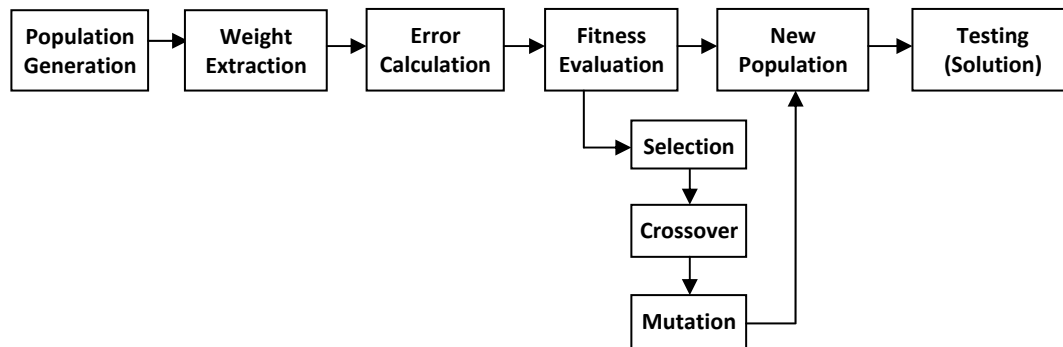


Figure 3: The block diagram of GA/BP based Hybrid Classifier

In genetic algorithm domain, a specific terminology based on natural genetics is followed [3]. The word ‘chromosome’ is used to represent the alternative solution for the problem. In present problem, features extracted from fruit images act as ‘genes’ and set of such genes form the chromosomes. Set of chromosomes further form the ‘population’ of alternative solutions. The term ‘weight’ signifies the importance assigned to inputs, fed to the network. ‘Error’ means difference in the forecasted and desired outputs. ‘Fitness’ is how close an individual (alternative solution) to the desired solution. More the fitness of the individual, more suitable candidate it is for the solution. Fitness is always inversely proportional to the error value. ‘Selection’ operator indicates finding the two fittest individuals out of population of alternatives. ‘Crossover’ operator implies merging of two parents (fittest alternatives) to reproduce a new offspring (new candidate solution). ‘Mutation’ operator means inculcating fresh features in the offspring to get diversity in the newly generated population.

The GA/BP NN algorithm works as follows:

- Step 1:** Generate random population of ‘p’ chromosomes (suitable solutions for the problem).
- Step 2:** Extract weights for input-hidden-output (l-m-n) layers from each chromosome x.
- Step 3:** Evaluate the fitness $f(x)$ of each chromosome x in the population by reciprocating the cumulative error values obtained for each input set (weather forecasting data).
- Step 4:** Create a new population by repeating following steps until the new population is complete
 - 4.1 Selection:** Select two parent chromosomes from a population according to their fitness (the better fitness, the bigger chance to be selected)
 - 4.2 Crossover:** Cross over the parents to form new offspring (children). If no crossover was performed, offspring is the exact copy of parents.
 - 4.3 Mutation:** With a mutation probability mutate new offspring at each position in chromosome.
 - 4.4 Acceptance:** Place the new offspring in the new population.
- Step 5:** Repeat steps 3 to 5 until stopping condition is met.

The output of classification step was in the form of text that specifies the class to which the fruit belonged to. Based on these classes, further grading was performed. The grading rules were: Assigning class A to non-defective fruit, class B to fruit having nominal surface defects and Class C to defective fruit. Hence, fruit grading was performed based on these rules.

IV. RESULTS AND DISCUSSION

An l-m-n architecture of 12-6-1 was used for simulation of neural networks as depicted in figure 4. The count of input neurons depends upon the number of feature extracted from the image, while the count of output neurons depend on the output values to be forecasted. For this scenario, the number of input neurons was 12 as the features extracted were 12 in count. Since, the network had shown minimum error values when number of hidden neurons were 6, so, $m=6$. Finally, the number of output neurons was taken as 1, because, there were three grading classes (Class A, Class B and Class C) and one of the three will be forecasted as output class.

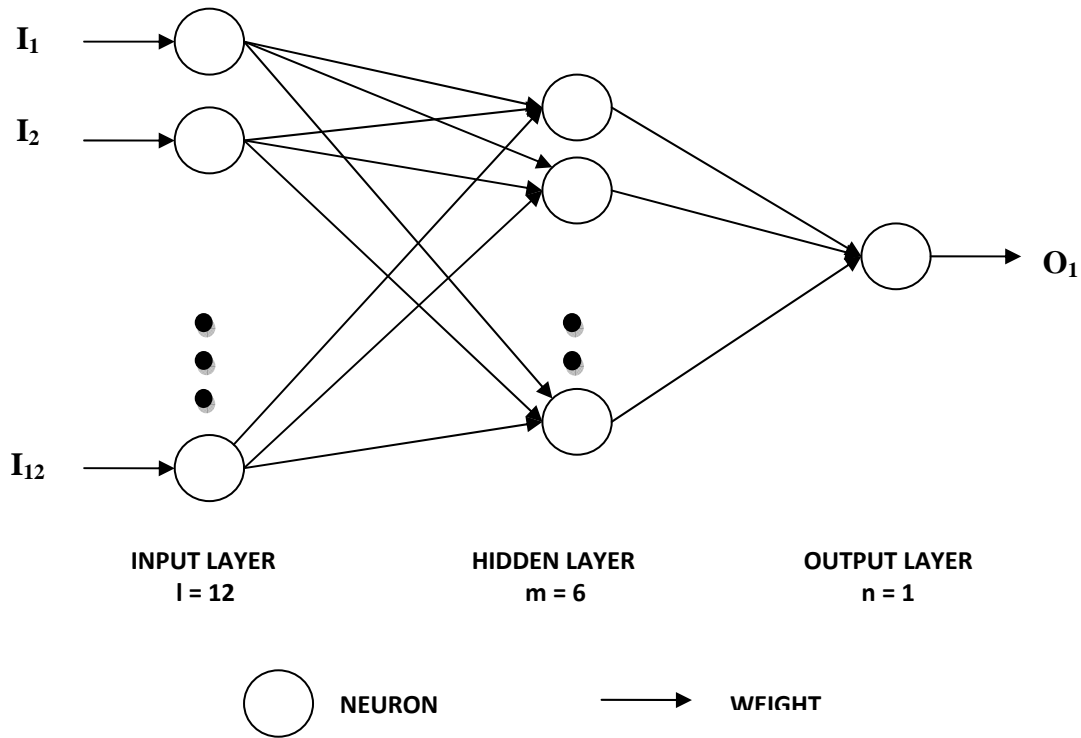


Figure 4: Neural Network Architecture for Fruit Grading Model







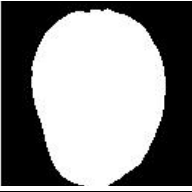
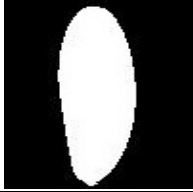
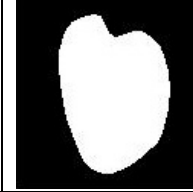
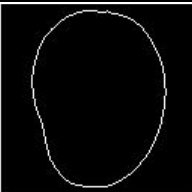
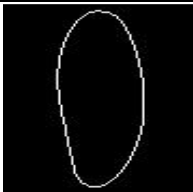

The GA/BP fruit model worked in two fractions: Training and Testing. In the training phase, the 12-6-1 network was trained for inputs as well as outputs (supervised learning) to obtain weights. These weights along with different input values were then fed to the network for testing. In this study, inputs were mango fruit images and outputs were grade classes: Grade A-C. From the total 50 images, 35 were used for training purposes while 15 images for testing.

A summary of various techniques applied at each step of the fruit grading model are provided in table 2. Outputs of three samples corresponding to five phases are depicted in the last three columns of the table. While analyzing the outputs, the images acquired from natural scene are converted to gray scale images and then enhanced by Wiener filter in pre-processing phase. Afterwards background is separated to obtain the fruit object from images using Otsu threshold based method. The output is binary images. Otsu segmentation is well suited for background subtraction purposes. However, it did not provide sufficient information regarding the fruit defects as it is visible in the table too. Consequently, another segmentation technique: Sobel edge operator was applied.

Then, the color and shape based features were obtained in the feature extraction phase. Here, color based features assisted in classifying raw or ripe mangoes so that the network could be trained to classify them. These were obtained directly from the RGB images. Shape based features were used to grade mangoes according to size and defects. Area, major axis, minor axis and eccentricity, all depicted the size of mangoes and were computed using the Otsu segmented image. Perimeter feature was utilized to extract the defect related information. It was computed both from Otsu segmented image (perimeter-O) and Sobel operator image (perimeter-S). The mango samples having surface defects had more difference in perimeter values, while, those with no defects were quite close. Using these features, the GA/BP NN was trained in the classification phase for 35 different images. After training, weights were extracted, which were fed along with new 15 images so as to grade them according to the rule discussed earlier.

In the table, sample 1 was graded as Class A because the mango had no surface defects and it is ripe. Sample 2 was classified as Class B, though it contained no surface defects but it was unripe (raw). The color based feature values depict the difference with the other two samples. Sample 3 was graded as Class C, since, it had surface defects. On comparing the perimeter-O and Primeter-S values for all the samples, it was obvious to put the sample 3 in Class C.

Table 2: Step-wise Outputs for Fruit Grading Model

Sr. no.	Phase	Technique Applied	Output of Phase		
			Sample 1	Sample 2	Sample 3
1.	Image Acquisition	Own Camera Setup			
2.	Pre-processing	Wiener Filter			
3.	Segmentation	Otsu Threshold based method			
		Sobel Edge Detection method			
4.	Feature Extraction	Color based Features			
		Mean_R	213.5776	188.2220	207.8598
		Mean_G	210.4785	212.7427	211.0254
		Mean_B	158.4328	207.7930	170.1105
		Std_R	24.5176	50.8604	29.2215
		Std_G	34.3755	41.9398	37.9538
		Std_B	97.2350	75.0643	89.0373
		Shape based Features			
		Area	7917	3698	7739
		Major axis	118.6926	118.6904	124.6422
		Minor axis	85.7838	39.9413	79.2224
		Eccentricity	0.6911	0.9417	0.7720
Perimeter-O	357.4630	274.5097	342.4924		
Perimeter-S	347.8061	275.9239	411.8478		
5.	Classification	GA/BP Neural Networks	GRADE: Class A	GRADE: Class B	GRADE: Class C

The error versus iteration graph for back propagation neural networks (BPNN) and GA/BP neural networks is shown in figure 5 and 6, respectively. It is quite evident from the graph that GA/BP NN converged to solution earlier than BPNN. It took less than 190 iterations for GA/BP to converge while BPNN took more than 200 iterations for the same. Probable reason for late convergence of BPNN might be that it got trapped into local minima. This further led to slow training. The constant line after 80th iteration, in figure 5, undoubtedly supported the fact that BPNN suffers from local minima problem. Also, it is evident from figure 6 that GA/BP had eliminated this problem for fruit grading model.

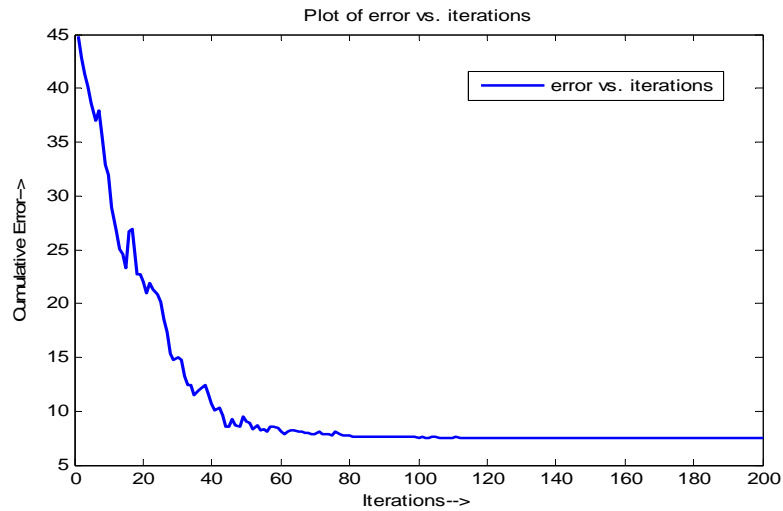


Figure 5: Error vs. Iteration graph for BPNN Approach

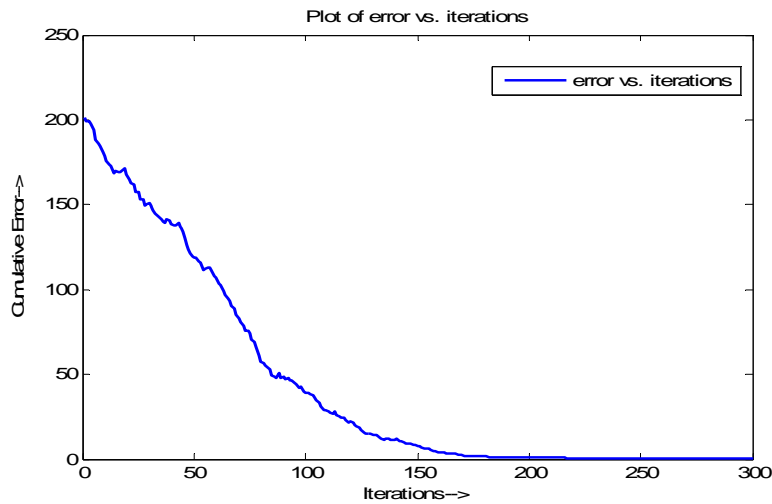


Figure 6: Error vs. Iteration graph for GA/BP NN Approach

In order to compare the proposed GA/BP NN based fruit grading model with BPNN models, a quantitative analysis was performed. Confusion matrices for both the models were formed after the testing phase. As discussed earlier, 15 mango fruit images were taken for testing. The test set was so designed to include 5 images for every grading class. This employs 5 images of Grade A, 5 images of Grade B and 5 images of Grade C. From the confusion matrices of figure 7(a) and (b), classification parameters were computed for both the models, provided in table 3. Two types of parameters were considered: one to determine the overall performance and other to evaluate grading class-wise performance. The former type included accuracy and misclassification rate while the latter were true positive rate, false Positive rate, specificity, precision, and prevalence.

Grading Class		Predicted Output		
		Grade A	Grade B	Grade C
Actual Output	Grade A	4	1	0
	Grade B	1	3	1
	Grade C	0	1	4

(a) Confusion matrix for BPNN

Grading Class		Predicted Output		
		Grade A	Grade B	Grade C
Actual Output	Grade A	5	0	0
	Grade B	0	4	1
	Grade C	0	0	5

(b) Confusion matrix for GA/BP NN

Figure 7: Confusion Matrix for Accuracy Evaluation- BPNN vs. GA/BP NN

Table 3: Performance Evaluation of BPNN and GA/BP NN Fruit Grading Models

Parameter	Formulas	Output value for BPNN			Output for GA/BP NN		
1. Accuracy	$\frac{\text{true positive} + \text{true negative}}{\text{total cases}}$	73.33%			93.33%		
2. Misclassification rate	$\frac{\text{false positive} + \text{false negative}}{\text{total cases}}$	26.67%			6.67%		
		Grade A	Grade B	Grade C	Grade A	Grade B	Grade C
3. True Positive rate	$\frac{\text{true positives}}{\text{actual positive cases}}$	80.0%	60.0%	80.0%	100%	80.0%	100%
4. False Positive rate	$\frac{\text{false positives}}{\text{actual negative cases}}$	10.0%	20.0%	10.0%	0.0%	10.0%	0%
5. Specificity	$\frac{\text{true negatives}}{\text{actual negative cases}}$	70.0%	80.0%	70.0%	90.0%	100%	90.0%
6. Precision	$\frac{\text{true positives}}{\text{forecasted positive cases}}$	36.4%	27.3%	36.4%	35.7%	28.6%	35.7%
7. Prevalence	$\frac{\text{actual positives}}{\text{total cases}}$	33.3%	33.3%	33.3%	33.3%	33.3%	33.3%

On analyzing the tabular values, it was manifested that GA/BP NN outperformed BPNN, showing an overall accuracy rate of 93.33%. Moreover, the misclassification rate was quite low for GA/BP NN (6.67%) as compared to BPNN (26.67%). Grading class-wise parameters also showed better results for GA/BP NN than BPNN alone.

V. CONCLUSIONS

Automation of fruit grading is quite significant for increased shelf life of fruit, maintenance of fruit quality and less human involvement. In this article, an accurate fruit grading system was presented in which artificial neural networks were hybridized with genetic algorithms so as to eliminate the drawbacks of back propagation algorithm. A five step procedure was followed for grading: image acquisition, pre-processing, segmentation, feature extraction and classification. The fruit were assigned grading classes (Class A, B and C) automatically according to grading rules. The model has shown remarkable performance when compared with the existing back propagation neural networks. It has achieved an accuracy rate of 93.3% in contrast to BPNN with only 73.3% accuracy. Thus, the GA/BP NN fruit grading model is proposed for future perspectives.

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